



Supporting Information

for

Naphthalimide-phenothiazine dyads: effect of conformational flexibility and matching of the energy of the charge-transfer state and the localized triplet excited state on the thermally activated delayed fluorescence

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General experimental methods, ^1H NMR, ^{13}C NMR, HRMS spectra of the compounds, theoretical computation data and the photophysical data

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1. General information

All the chemicals used in synthesis are analytically pure and were used as received. Solvents were dried and distilled prior to use. ^1H and ^{13}C NMR spectra were recorded on Bruker Avance spectrometers (400/500/600 MHz). ^1H and ^{13}C chemical shifts are reported in parts per million (ppm) relative to TMS, with the residual solvent peak used as an internal reference. The mass spectra were measured by HRMS (MALDI-TOF, recorded on a Bruker Ultraflextreme mass spectrometer) and HRMS (ESI-TOF, recorded on an Agilent G6224A mass spectrometer). UV-vis absorption spectra were measured on a UV-2550 UV-vis spectrophotometer (Shimadzu Ltd., Japan). Fluorescence spectra were recorded with an FS5 spectrofluorometer (Edinburgh instruments, UK). Luminescence lifetimes of compounds were recorded with an OB920 luminescence lifetime spectrometer (Edinburgh Instruments, U.K.). All these calculations were performed with Gaussian 09W [1]. Natural transition orbital analysis were performed by the Multiwfn program [2].

2. Synthesis of the compounds

2.1. Synthesis of **2.** Compound **2** was synthesized in a manner similar to [3]. A mixture of **NI-3Br** (3.0 g, 7.750 mmol), bis(pinacolato)diboron (2.0 g, 7.750 mmol), KOAc (1.5 g, 15.5 mmol) and Pd(dppf)Cl₂ (257.4 mg, 0.320 mmol) in toluene (77mL) was degassed by gently bubbling N₂ for 30 min. The mixture was then stirred at 110 °C for 16 h. After cooling, the mixture was extracted with CH₂Cl₂ (100 mL × 3). The combined organic layer was washed with water (100 mL), brine solution (100 mL), dried over anhydrous Na₂SO₄, filtered, and evaporated to dryness. The crude product was purified by column chromatography (silica gel, DCM/PE 1:6, v/v) to give product **2** as white solid (400 mg, 11.9%). ^1H NMR (400 MHz CDCl₃) δ : 0.86–0.94 (m, 6H), 1.30–1.37 (m, 8H), 1.40 (s, 12H), 1.92–1.96 (m, 1H), 4.08–4.19 (m, 2H), 7.75 (m, J = 15.51 Hz, 1H), 8.23 (d, J = 8.13 Hz, 1H), 8.62 (d, J = 25.01 Hz, 1H), 8.67 (s, 1H), 8.99 (s, 1H). ^{13}C NMR (125 MHz, CDCl₃) δ : 164.63, 164.46, 138.00, 136.49, 134.07, 132.22, 131.73, 130.20, 127.84, 126.86, 123.82,

122.79, 84.56, 44.18, 37.96, 30.80, 28.77, 24.95, 24.13, 23.09, 10.58. HRMS (MALDI, *m/z*) calcd for C₃₈H₃₄N₂O₂S [M+H]⁺, 435.2581, found 436.2665.

2.2. Synthesis of NI-Ph-Br. Under a N₂ atmosphere, compound **2** (61.1 mg, 0.141 mmol) and 1-bromo-4-iodobenzene (75.0 mg, 0.265 mmol) were dissolved in mixed solvent of toluene (3 mL), ethanol (0.8 mL) and water (0.5 mL), followed by the addition of K₂CO₃ (70.0 mg, 0.506 mmol). After bubbling with N₂ for 20 min, Pd(PPh₃)₄ (30 mg, 0.026 mmol) was added, and the mixture was refluxed for 8 h. Then, the reaction mixture was cooled to room temperature and extracted with dichloromethane. The organic layer was dried over anhydrous Na₂SO₄ and concentrated under reduced pressure to attain the crude product. The residue was purified by column chromatography (silica gel, DCM/PE 1:2, v:v) to afford compound **NI-Ph-Br** as pale white solid (64 mg, 92.9%). ¹H NMR (400 MHz, CDCl₃) δ : 0.88–0.96 (m, 6H), 1.31–1.41 (m, 8H), 1.94–1.97 (m, 1H), 4.10–4.20 (m, 2H), 7.66 (s, 4H), 7.79 (m, *J* = 15.25 Hz, 1H), 8.25 (d, *J* = 8.00 Hz, 1H), 8.35 (s, 1H), 8.60 (d, *J* = 7.25 Hz, 1H), 8.83 (s, 1H). ¹³C NMR (125 MHz, CDCl₃) δ : 164.46, 138.85, 138.20, 133.88, 132.36, 132.12, 131.19, 130.93, 130.28, 128.98, 127.53, 123.46, 122.80, 44.25, 38.00, 30.80, 29.71, 28.75, 10.68, 8.83. HRMS (MALDI, *m/z*) calcd for C₂₆H₂₆BrNO₂ [M+H]⁺, 463.1147, found 464.1220.

2.3. Synthesis of 3. Compound **2** (300.0 mg, 0.690 mmol) and 5-bromo-2-iodo-1,3-dimethylbenzene (300 mg, 0.965 mmol) were dissolved in a deaerated mixed solvent containing toluene (7 mL), ethanol (2 mL), and water (1 mL). After the addition of the catalysts Pd(PPh₃)₄ (79.6 mg, 0.069 mmol) and potassium carbonate (285.7 mg, 2.067 mmol), the mixture was stirred for 15 min at room temperature. Then, the reaction suspension was heated to 78 °C and this reaction temperature was kept for 1 h. Following that the reaction temperature was further increased to 110 °C and stirring continued for additional 9 h. Then, the reaction mixture was allowed to cool to room temperature, extracted with chloroform, washed with water and brine. The combined organic layer was dried by anhydrous Na₂SO₄ and concentrated under reduced pressure. The residue was purified by column chromatography (silica gel, DCM/PE 1:4, v:v). Compound **3** was obtained as pale white solid **3** (150 mg, 60.6%). ¹H NMR (400 MHz, CDCl₃) δ : 0.86–0.96 (m, 6H), 1.29–1.42 (m, 8H), 1.93–1.98 (m, 1H), 2.02

(s, 6H), 4.08–4.19 (m, 2H), 7.33 (s, 2H), 7.80 (m, J = 15.51 Hz, 1H), 7.96 (d, J = 1.50 Hz, 1H), 8.20 (d, J = 8.13 Hz, 1H), 8.38 (d, J = 1.50 Hz, 1H), 8.63 (d, J = 7.26 Hz, 1H). ^{13}C NMR (125 MHz, CDCl_3) δ : 164.51, 138.88, 138.23, 133.89, 132.37, 131.20, 130.31, 128.99, 127.54, 127.44, 123.48, 122.85, 44.25, 38.01, 30.81, 28.75, 24.11, 23.09, 14.11, 10.68. HRMS (MALDI, m/z) calcd for $\text{C}_{28}\text{H}_{30}\text{BrNO}_2$ [M+H] $^+$, 491.1460, found 492.1533.

3. Molecular structure characterization data

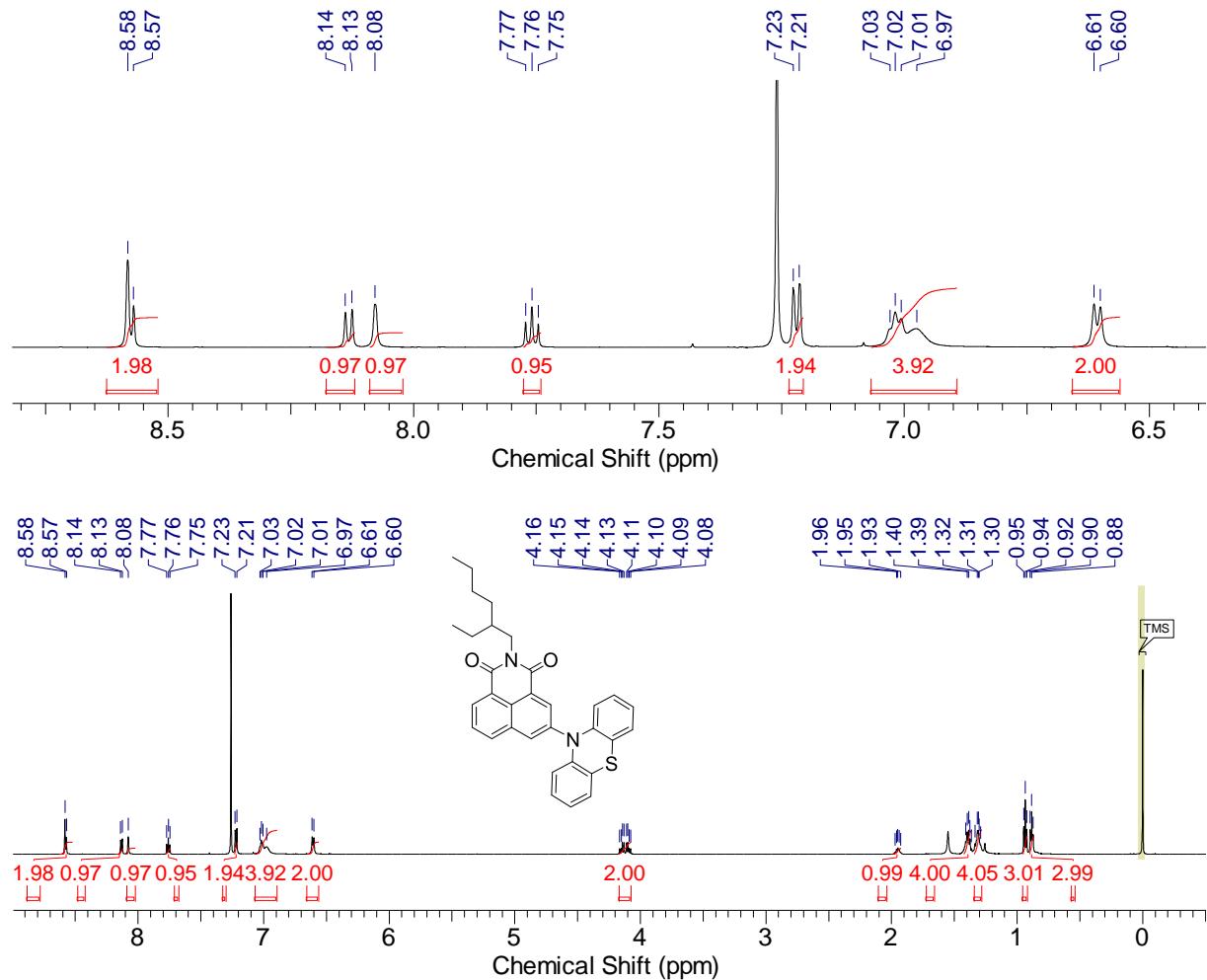


Figure S1. ^1H NMR spectrum of **NI-PTZ** in CDCl_3 (400 MHz), 25 °C.

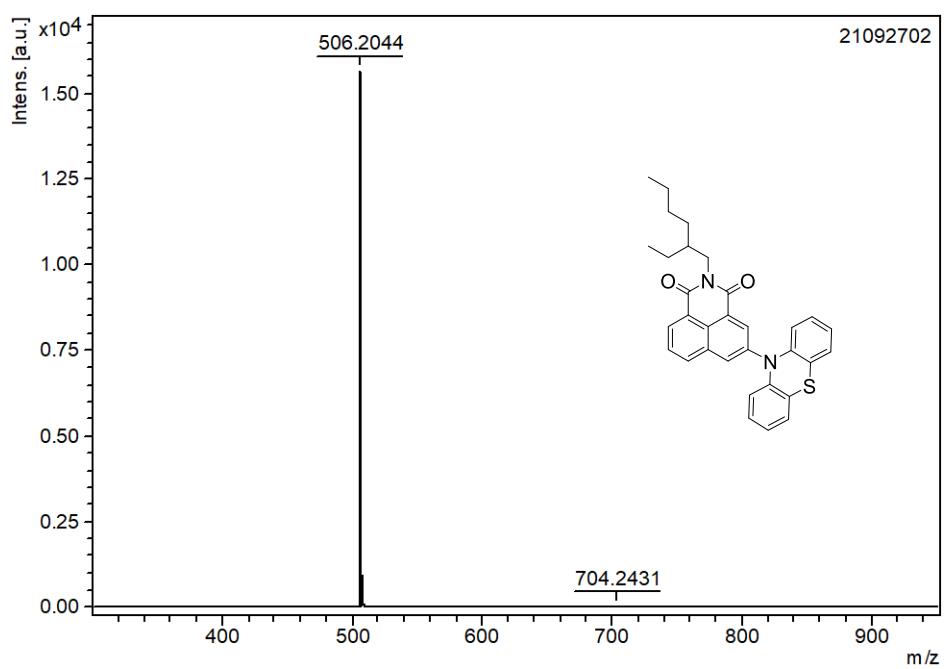


Figure S2. MALDI-HRMS spectrum of **NI-PTZ**, 25 °C.

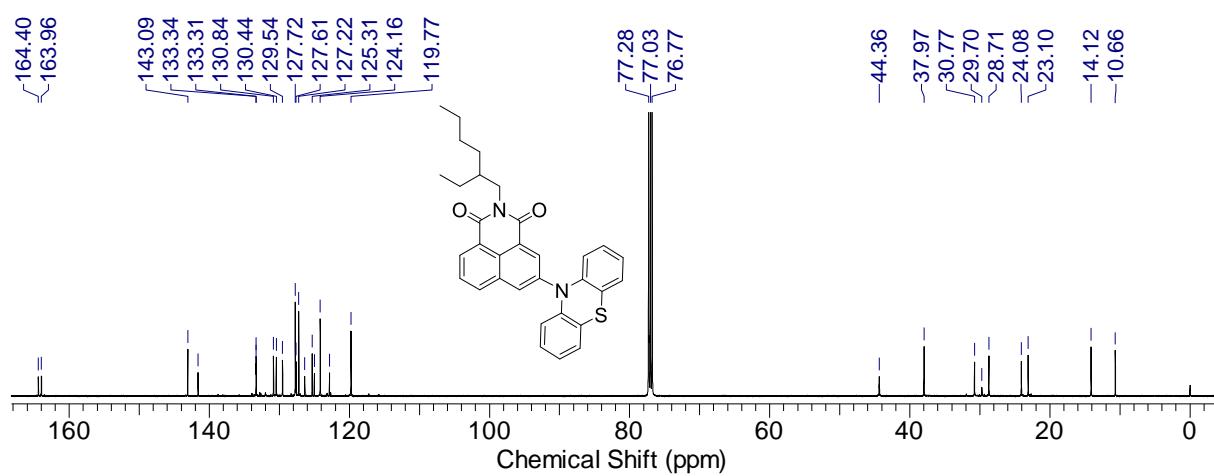


Figure S3. ^{13}C NMR spectrum of **NI-PTZ** in CDCl_3 (125 MHz), 25 °C.

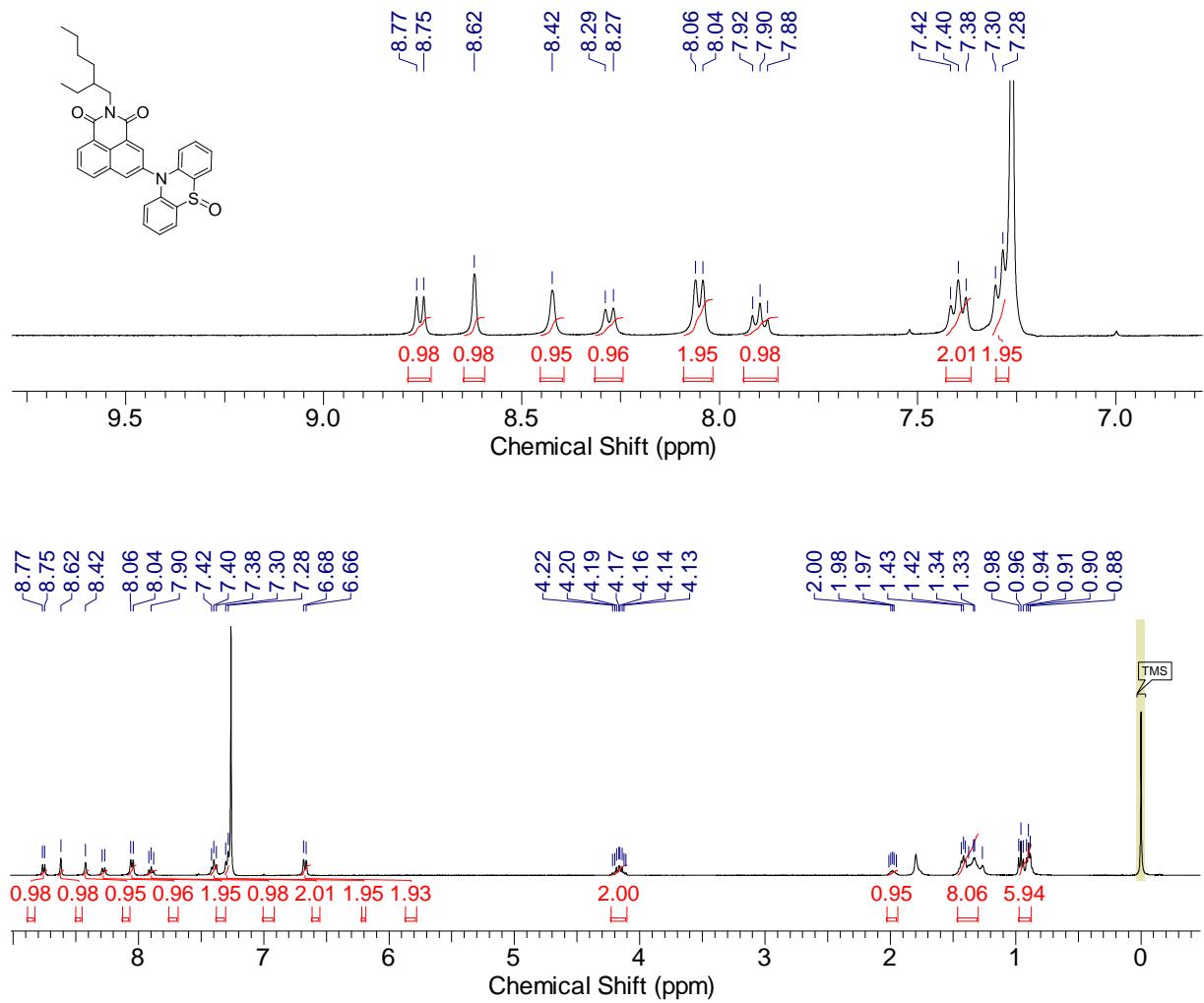


Figure S4. ^1H NMR spectrum of **NI-PTZ-O** in CDCl_3 (400 MHz), 25 °C.

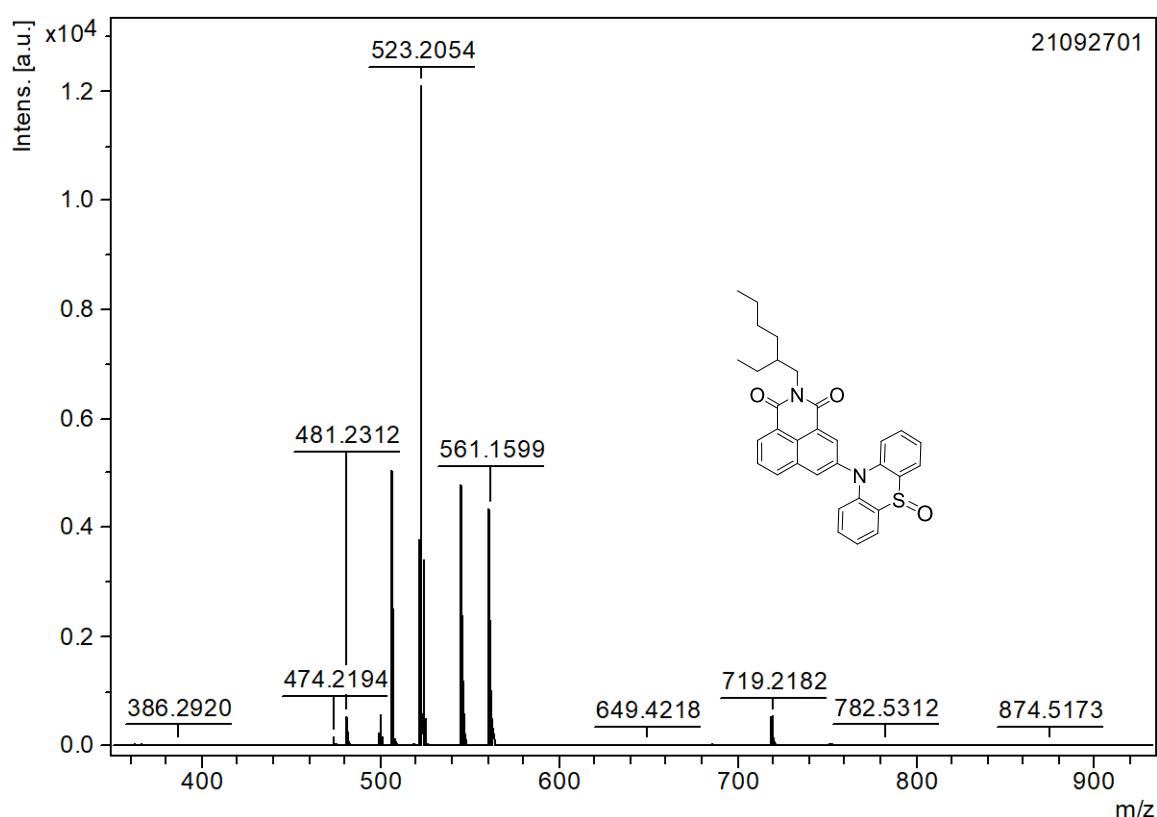


Figure S5. MALDI-HRMS spectrum of **NI-PTZ-O**, 25 °C.

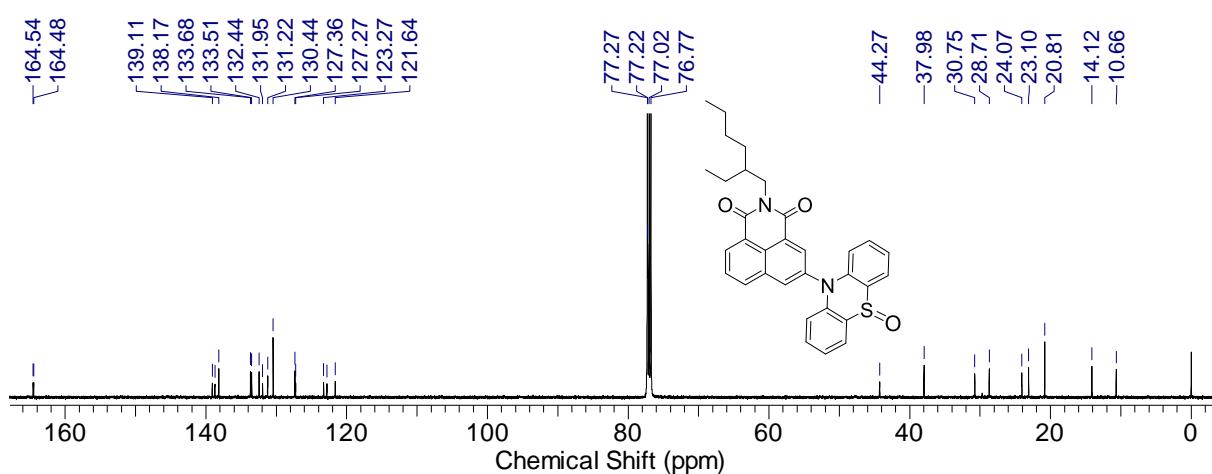


Figure S6. ^{13}C NMR spectrum of **NI-PTZ-O** in CDCl_3 (125 MHz), 25 °C.

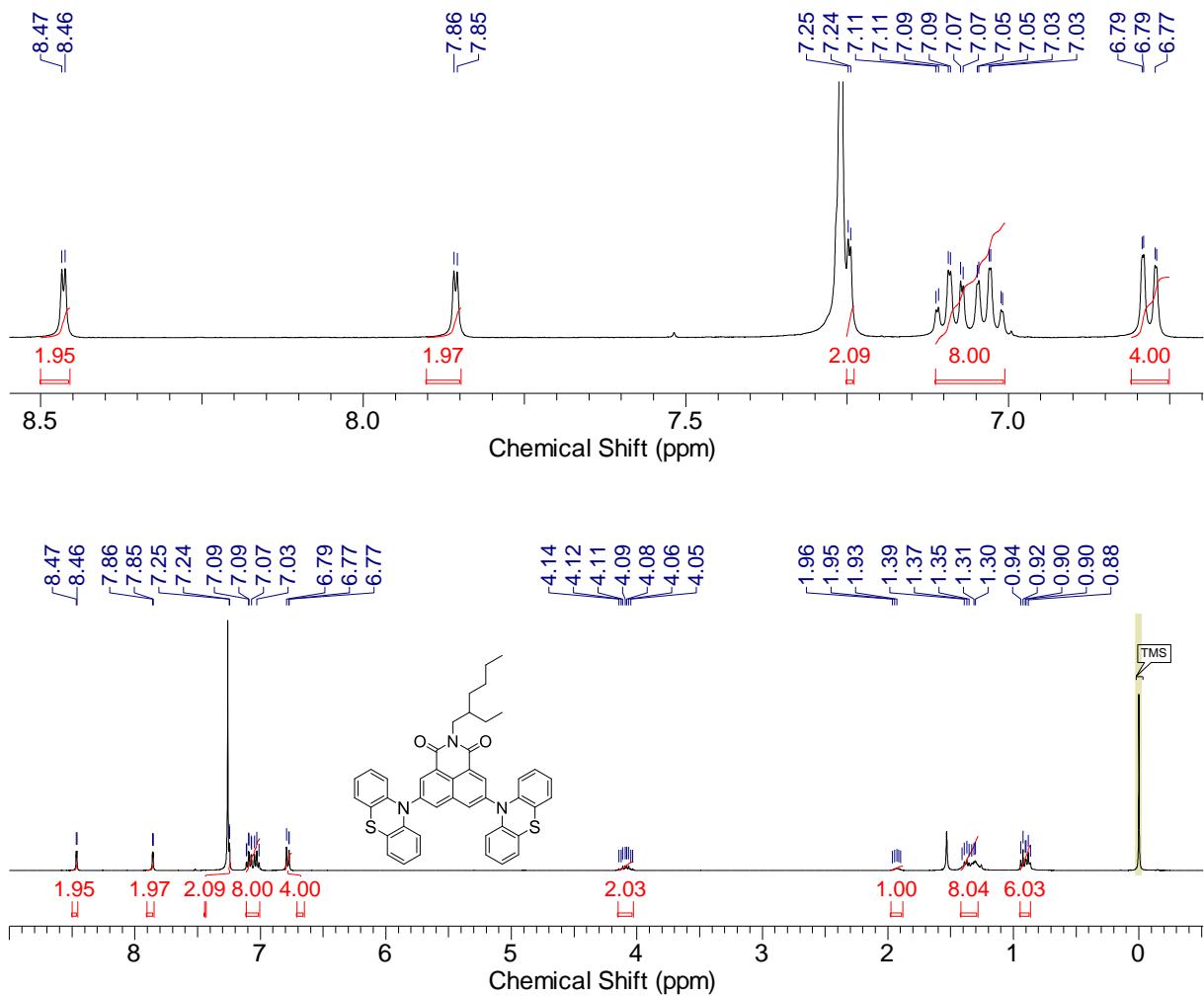


Figure S7. ¹H NMR spectrum of NI-PTZ₂ in CDCl₃ (400 MHz), 25 °C.

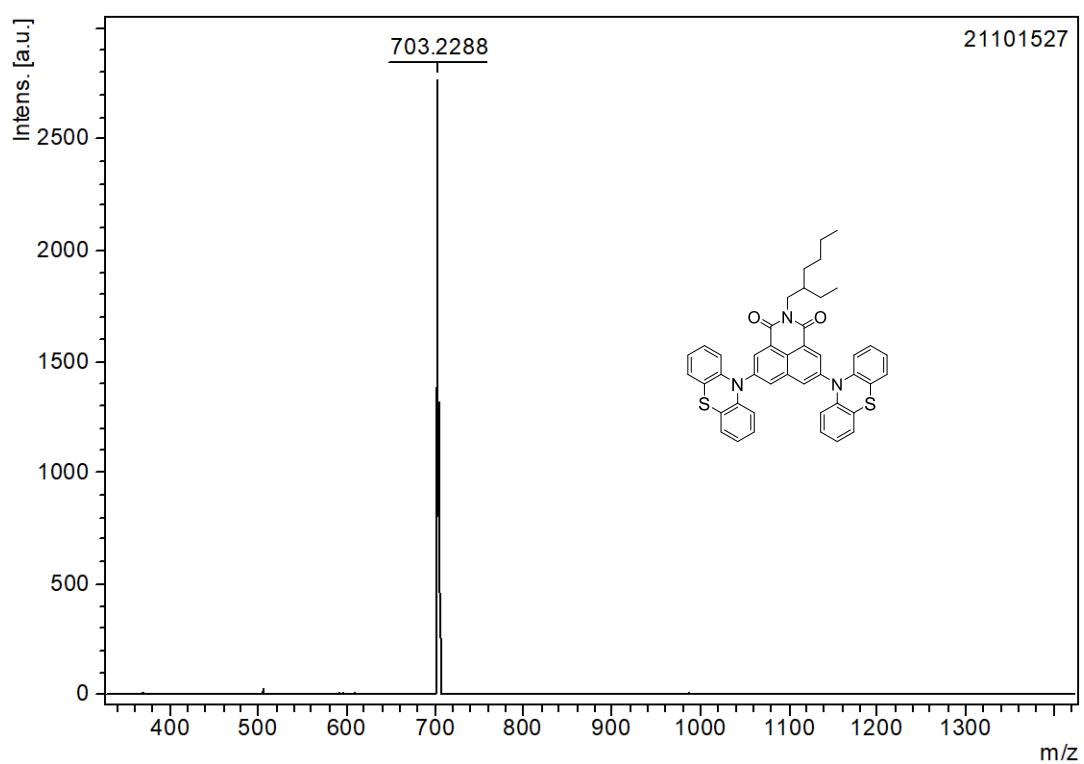


Figure S8. MALDI-HRMS spectrum of **NI-PTZ₂**, 25 °C.

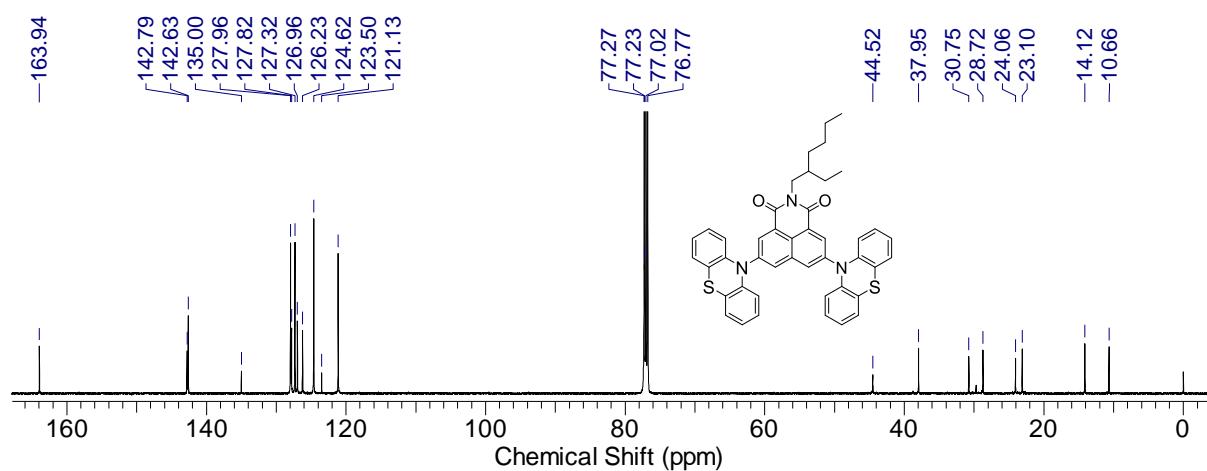


Figure S9. ¹³C NMR spectrum of **NI-PTZ₂** in CDCl₃ (125 MHz), 25 °C.

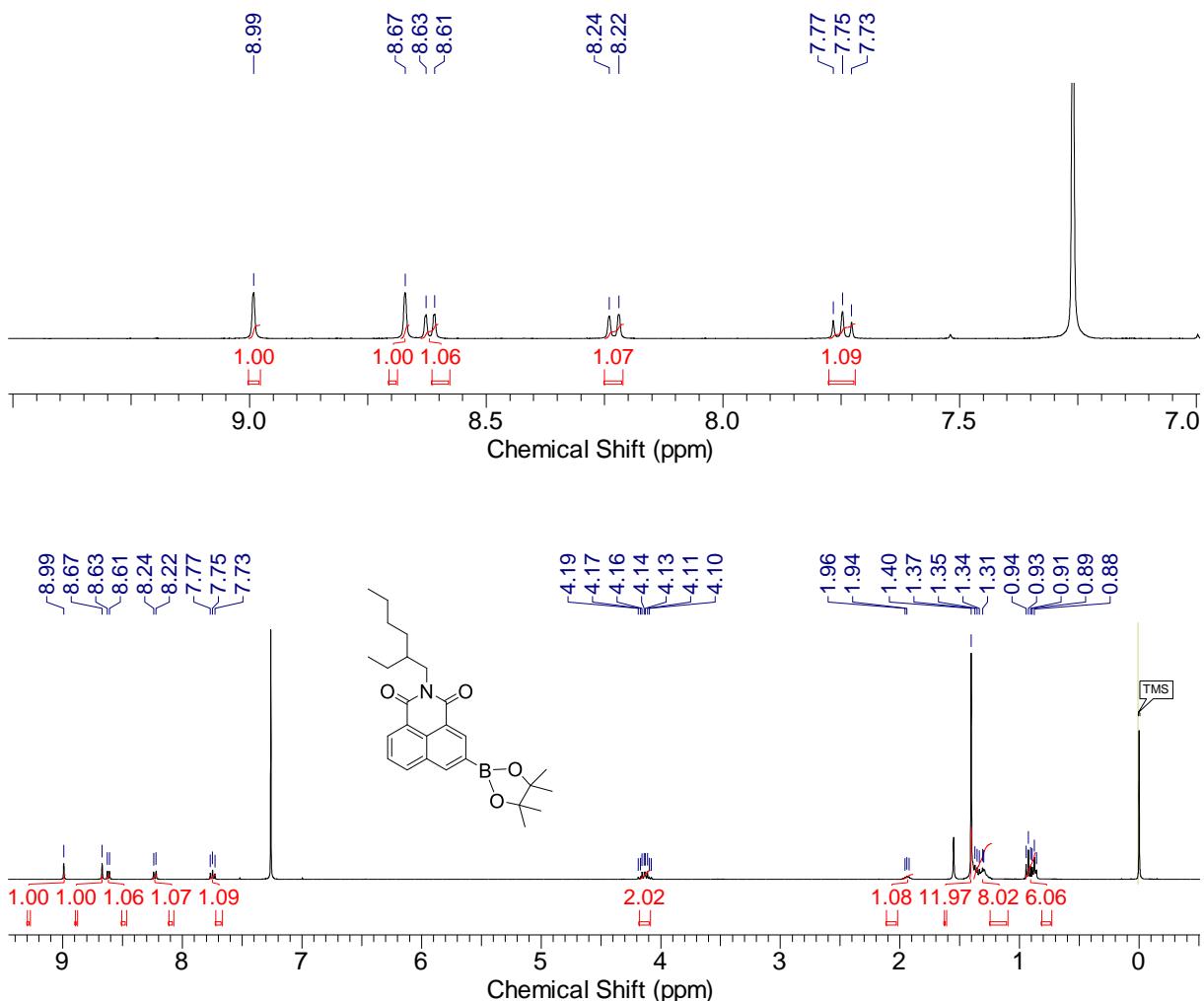


Figure S10. ^1H NMR spectrum of **2** in CDCl_3 (400 MHz), 25 °C.

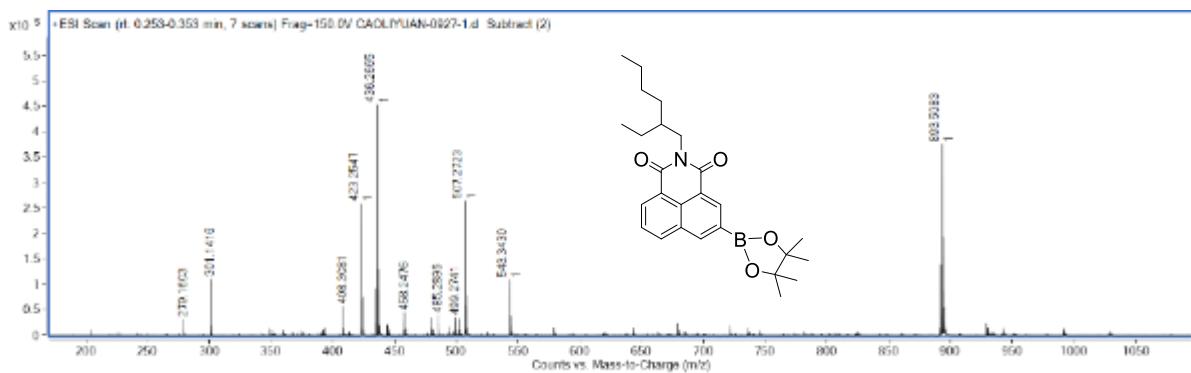


Figure S11. ESI-HRMS spectrum of **2**, 25 °C.

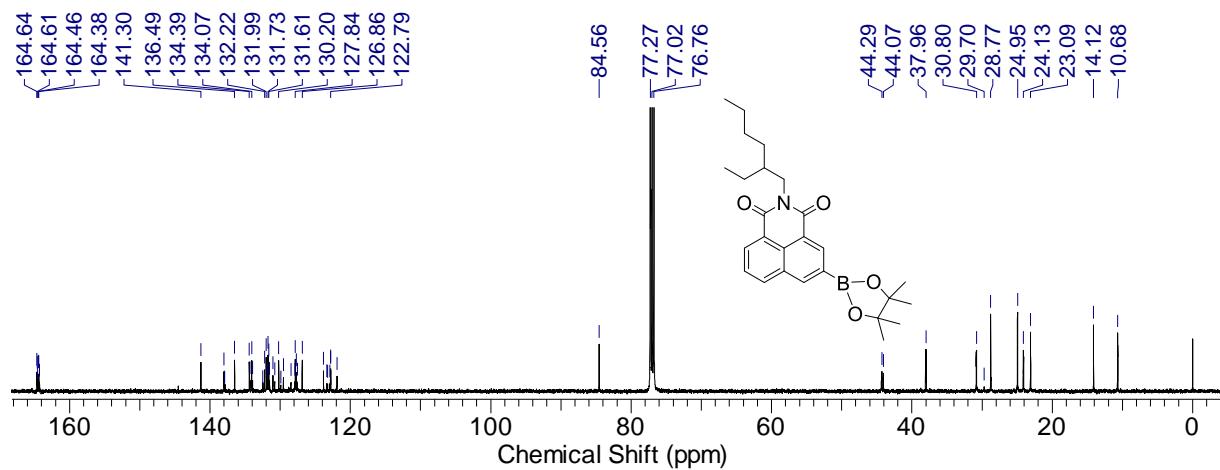


Figure S12. ^{13}C NMR spectrum of **2** in CDCl_3 (125 MHz), 25 °C.

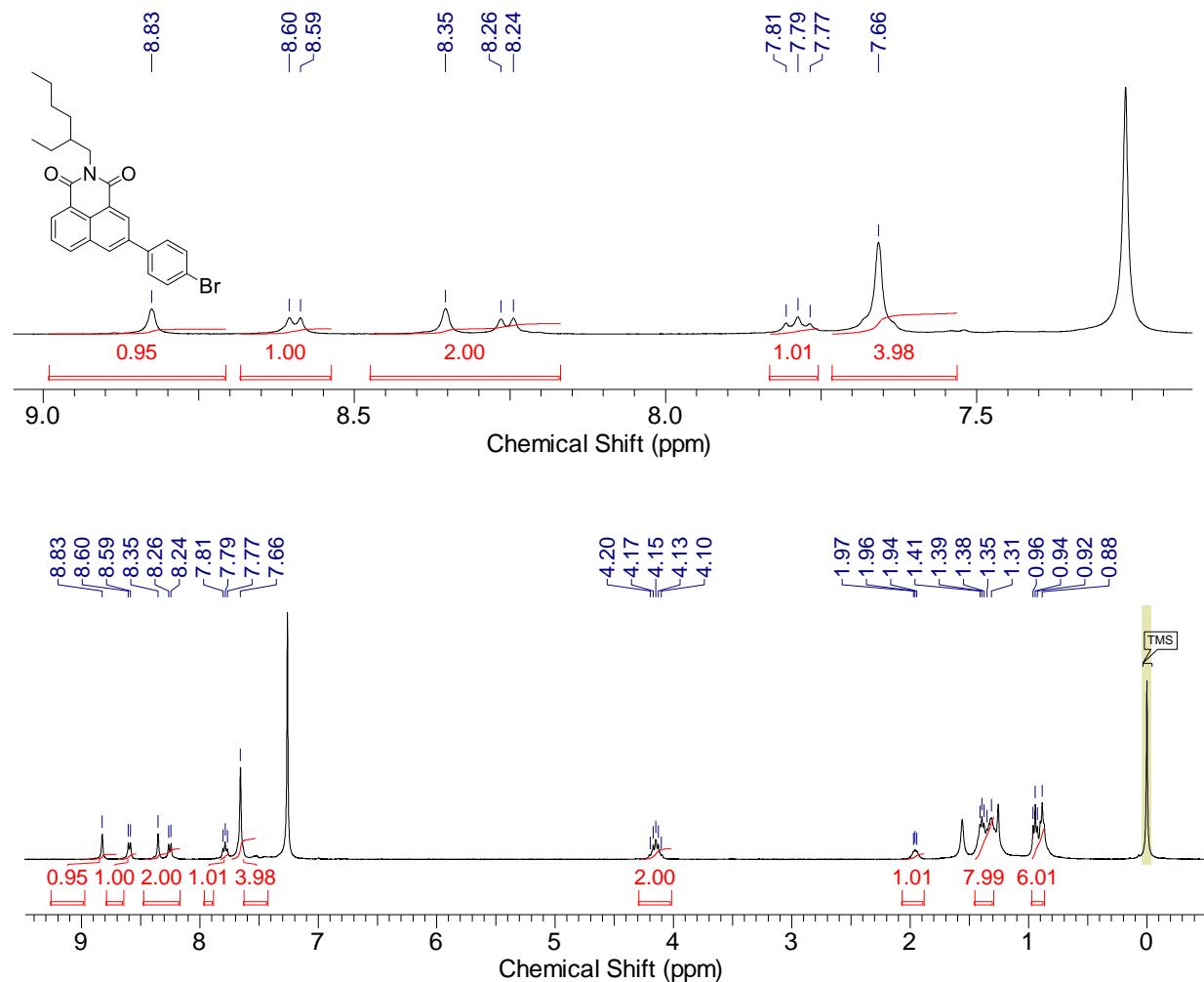


Figure S13. ^1H NMR spectrum of **NI-Ph-Br** in CDCl_3 (400 MHz), 25 °C.

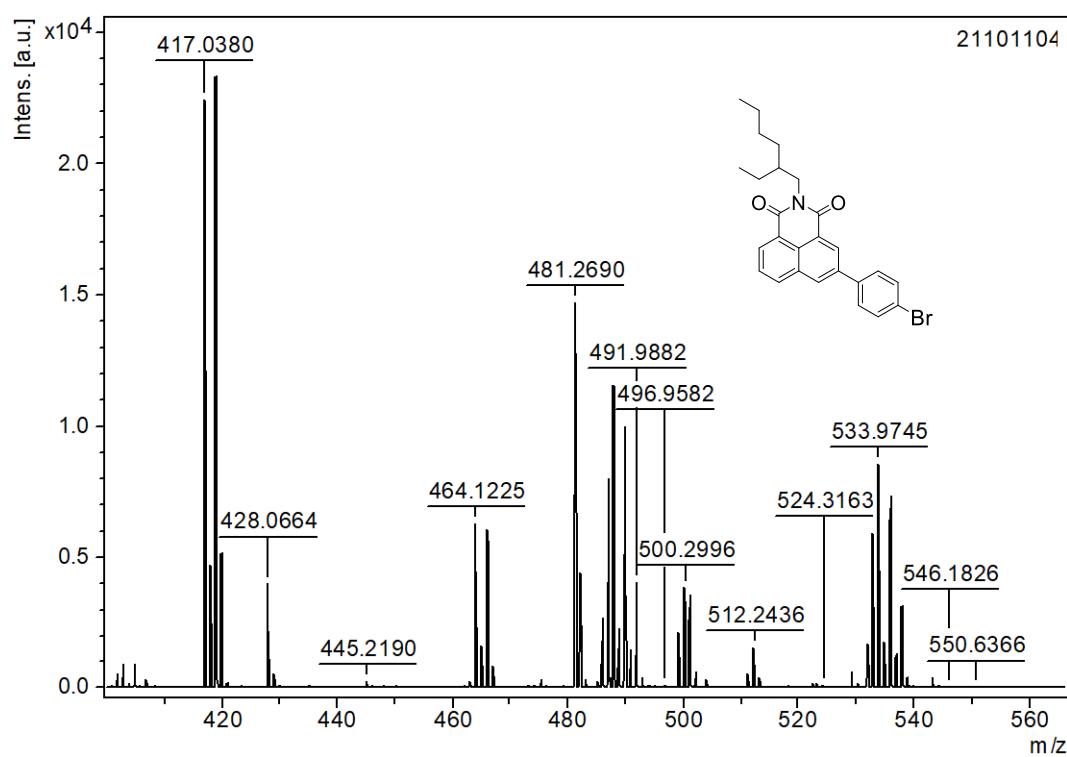


Figure S14. MALDI-HRMS spectrum of **NI-Ph-Br**, 25 °C.

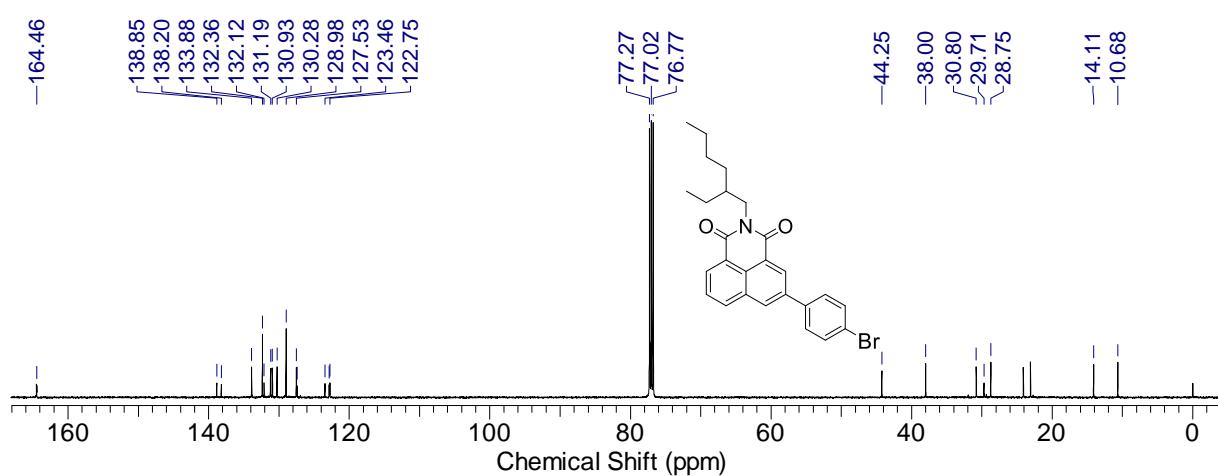
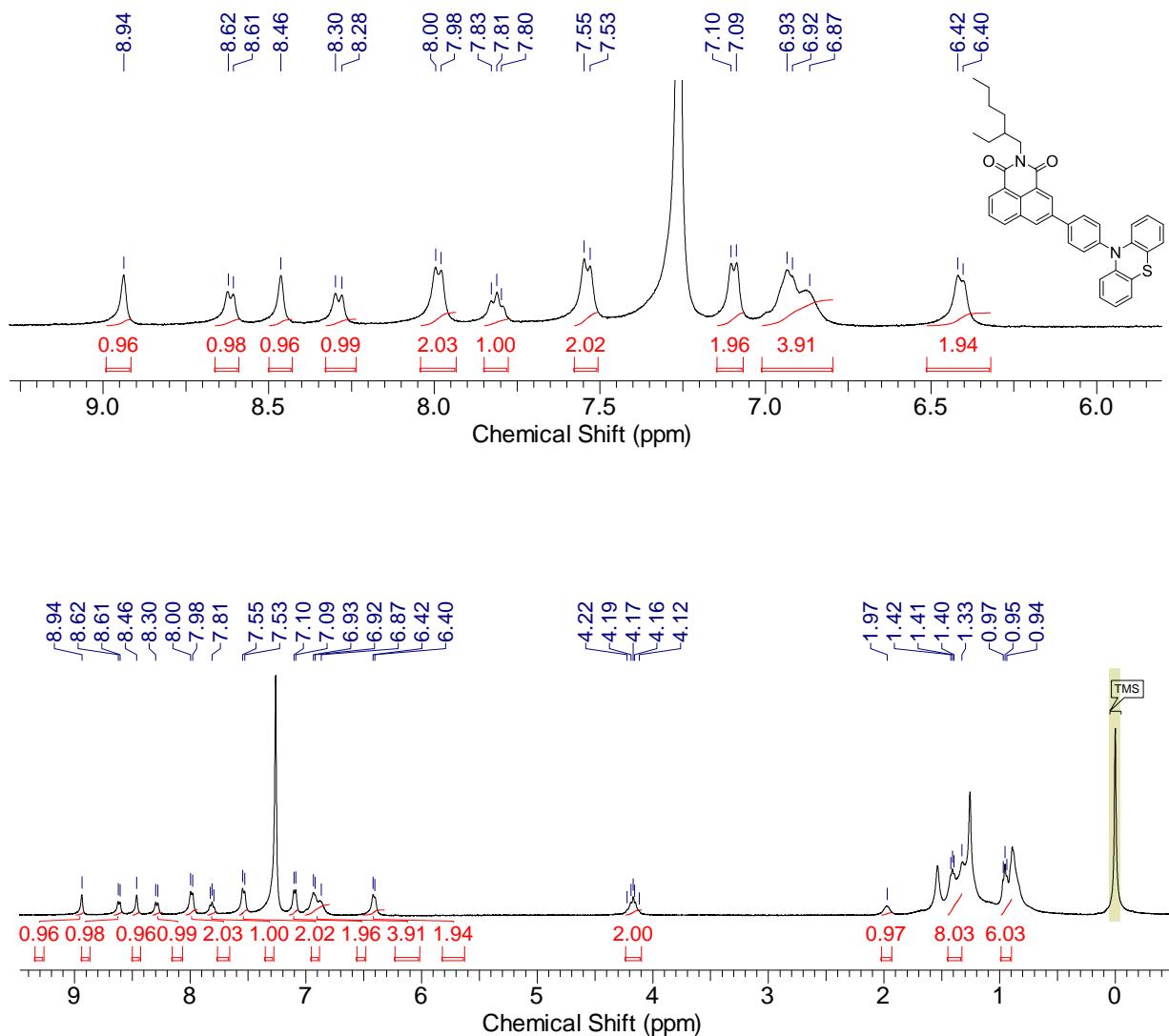


Figure S15. ^{13}C NMR spectrum of **NI-Ph-Br** in CDCl_3 (125 MHz), 25 °C.



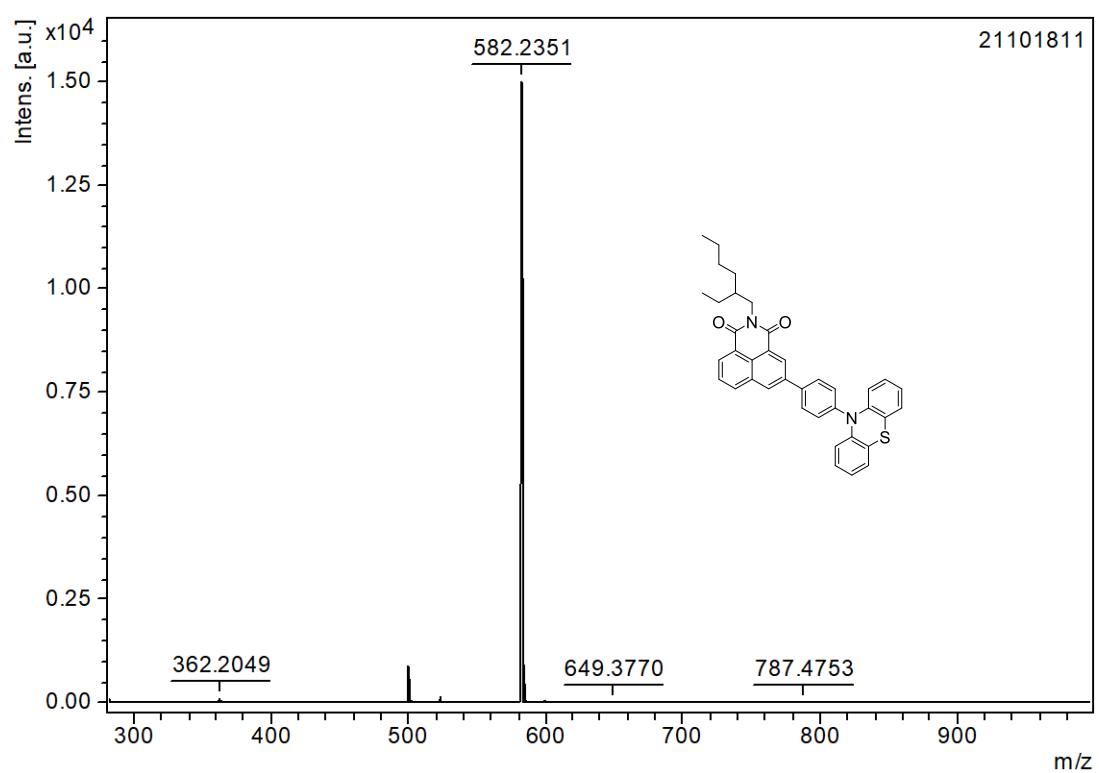


Figure S17. MALDI-HRMS spectrum of **NI-Ph-PTZ**, 25 °C.

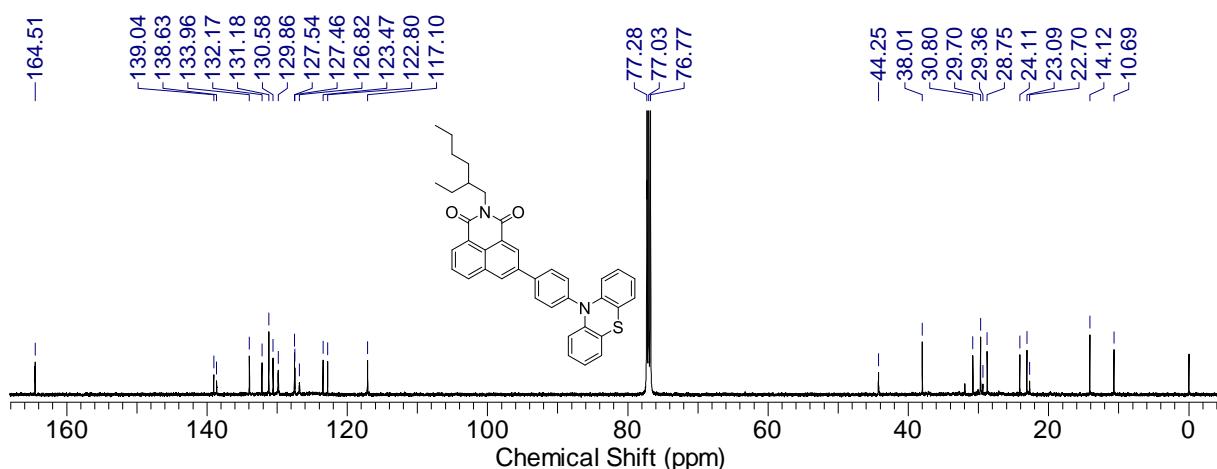


Figure S18. ^{13}C NMR spectrum of **NI-Ph-PTZ** in CDCl_3 (125 MHz), 25 °C.

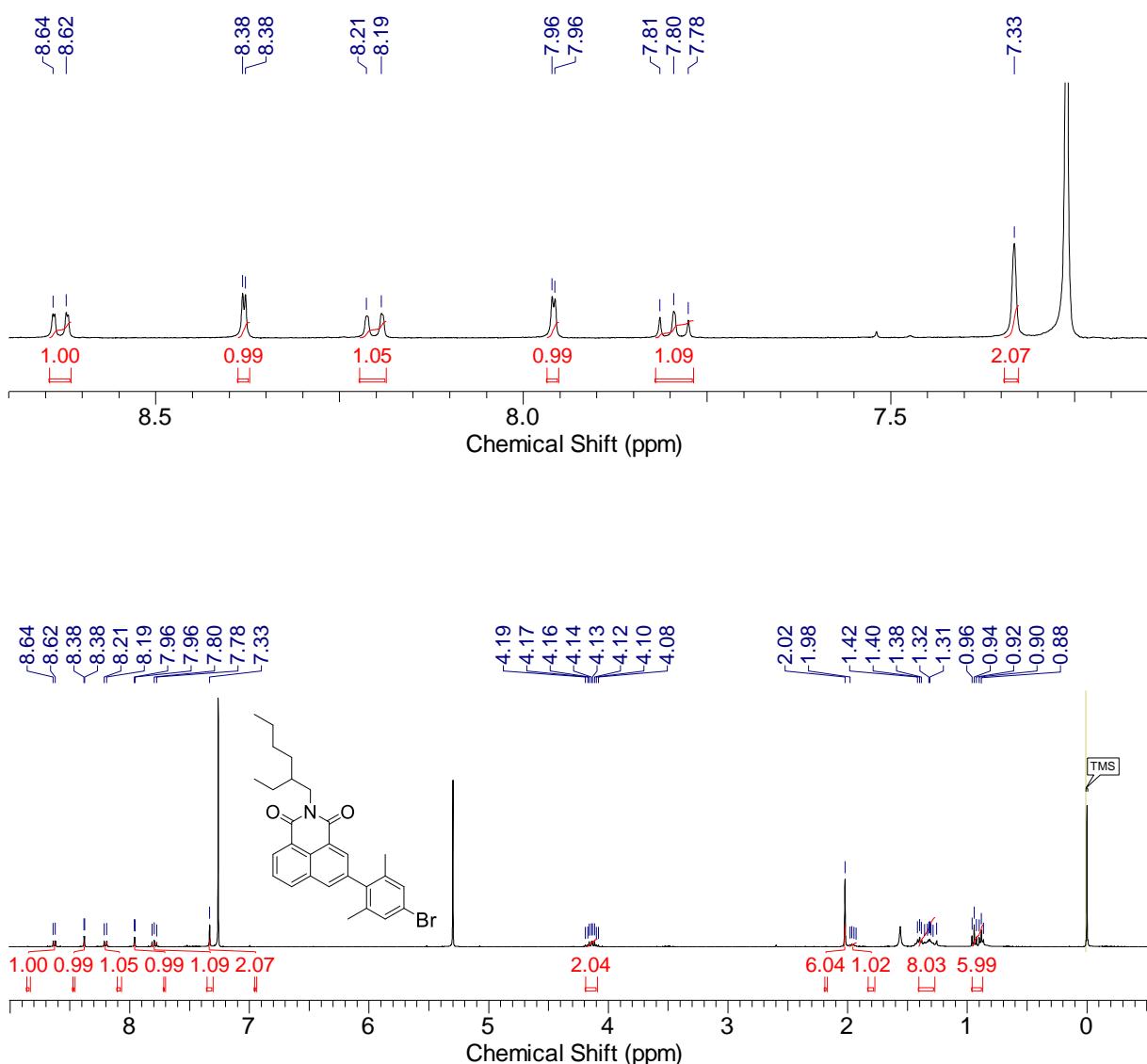


Figure S19. ^1H NMR spectrum of **3** in CDCl_3 (400 MHz), 25 °C.

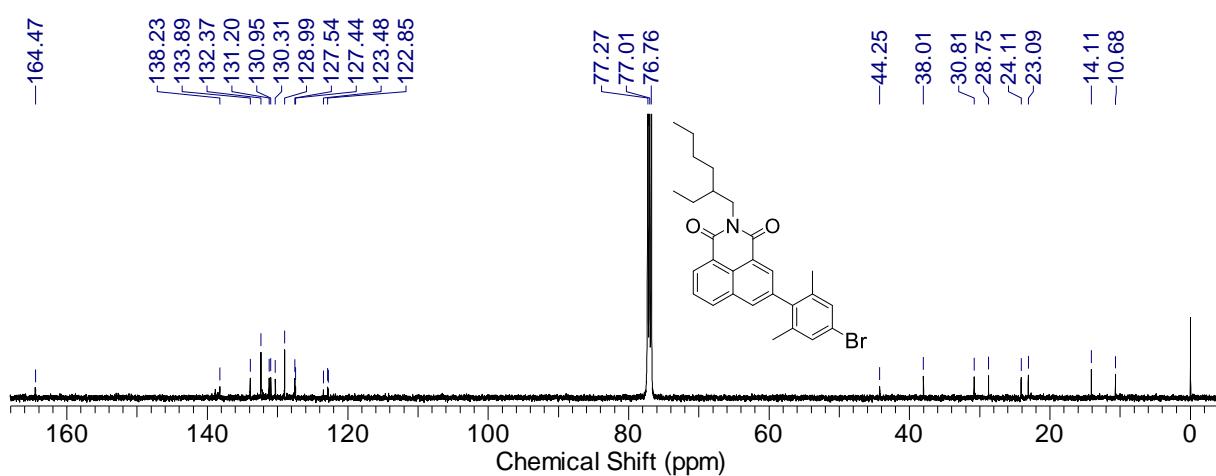
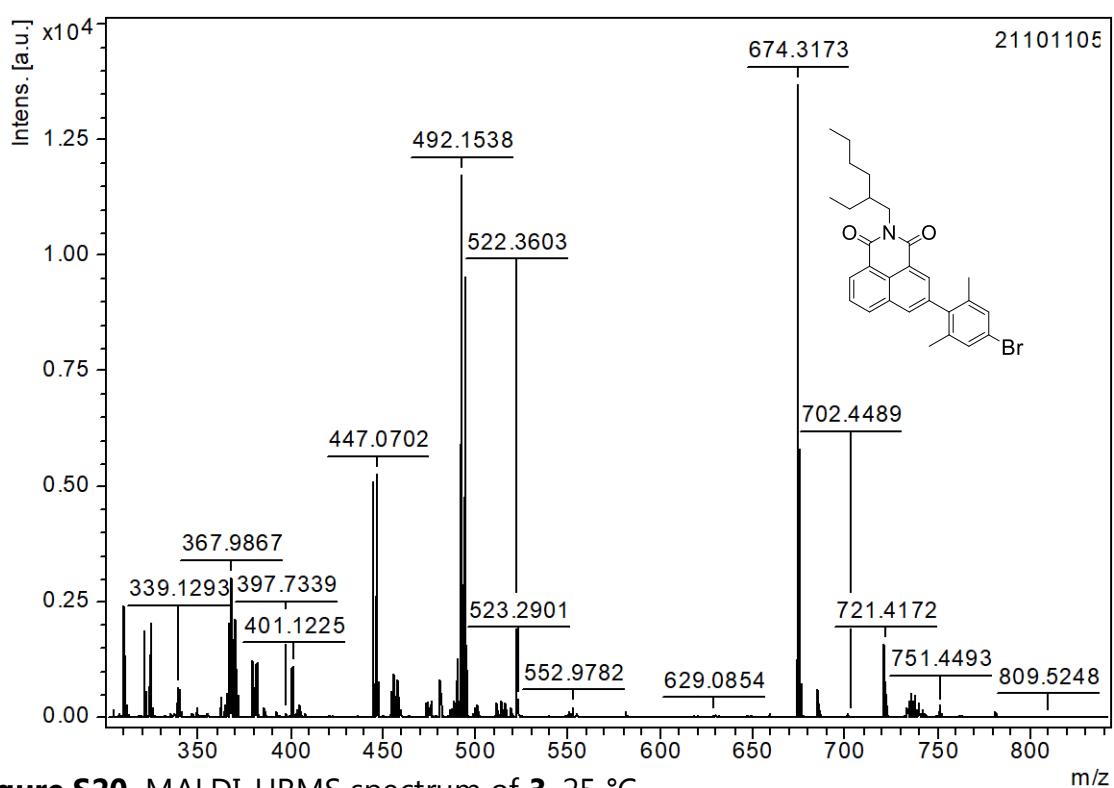


Figure S21. ^{13}C NMR spectrum of **3** in CDCl_3 (125 MHz), 25 °C.

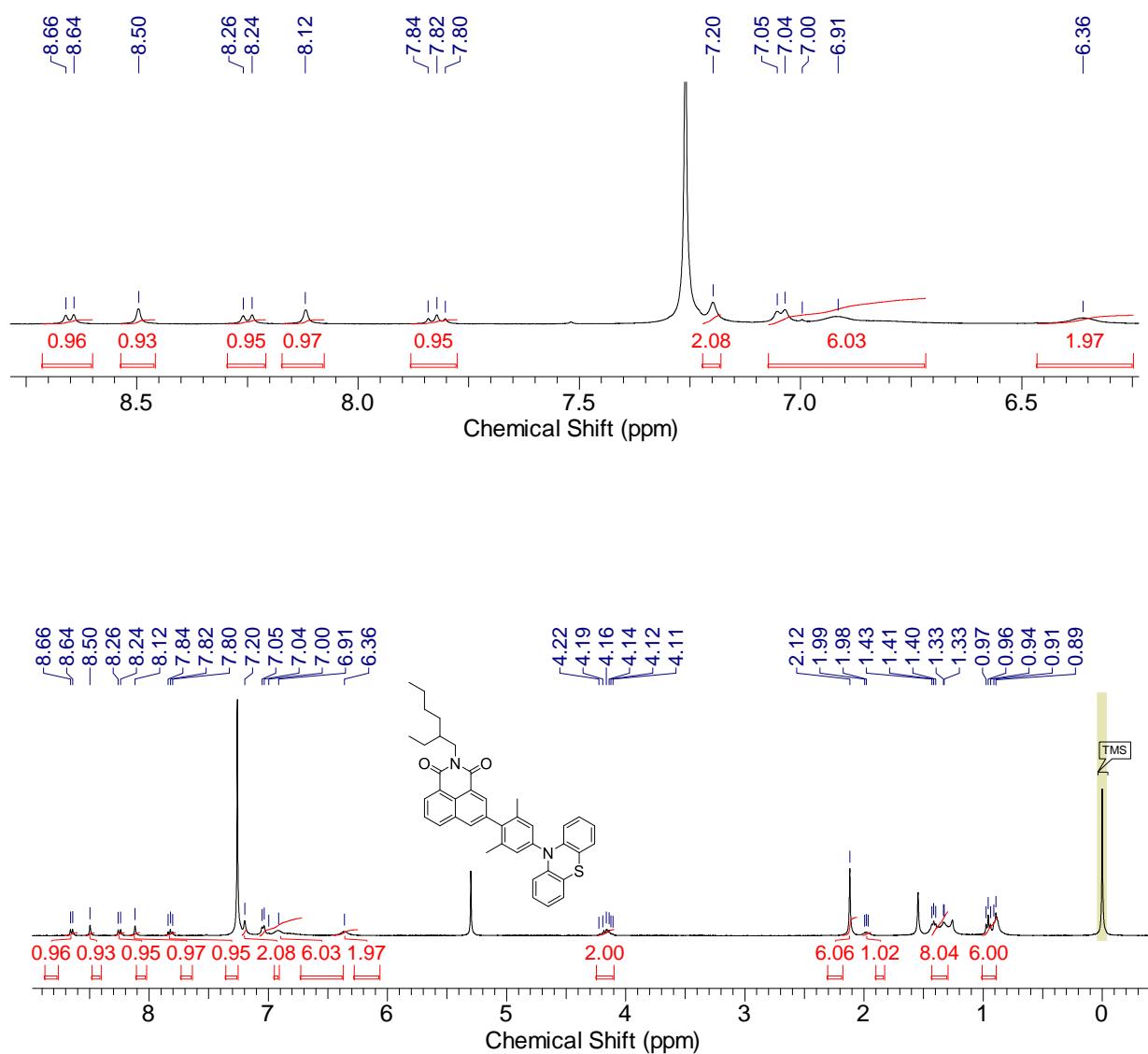


Figure S22. ^1H NMR spectrum of NI-PhMe₂-PTZ in CDCl_3 (400 MHz), 25 °C.

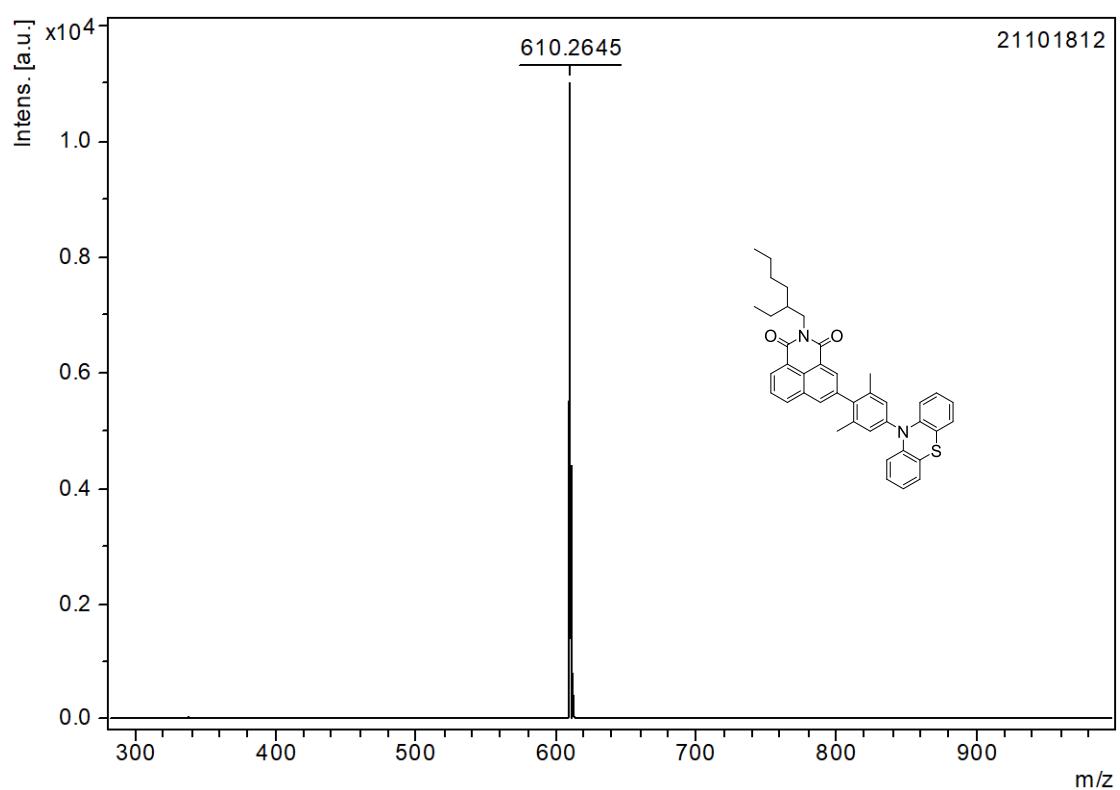


Figure S23. MALDI-HRMS spectrum of **NI-PhMe₂-PTZ**, 25 °C.

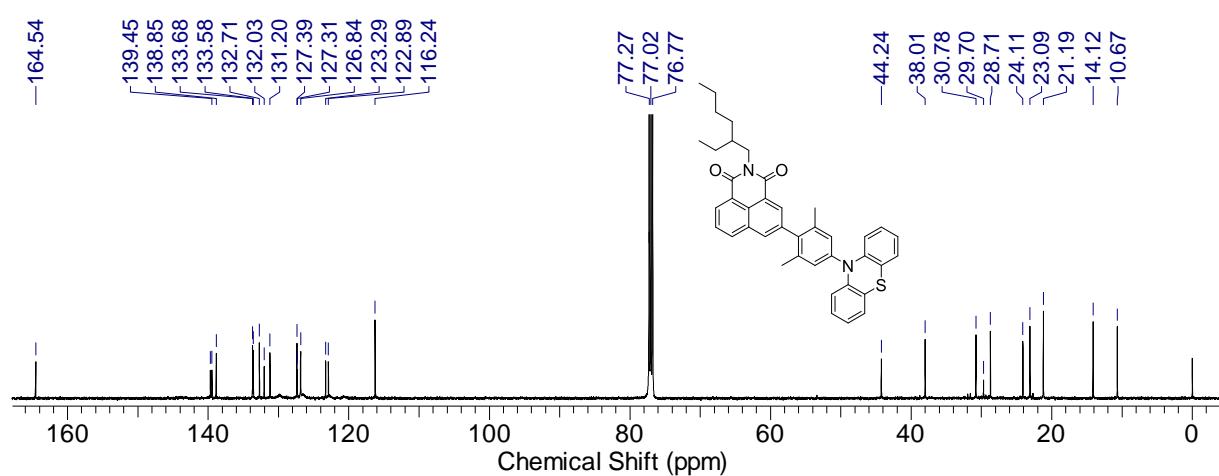


Figure S24. ¹³C NMR spectrum of **NI-PhMe₂-PTZ** in CDCl₃ (125 MHz), 25 °C.

4. Steady state UV-vis absorption and luminescence spectra

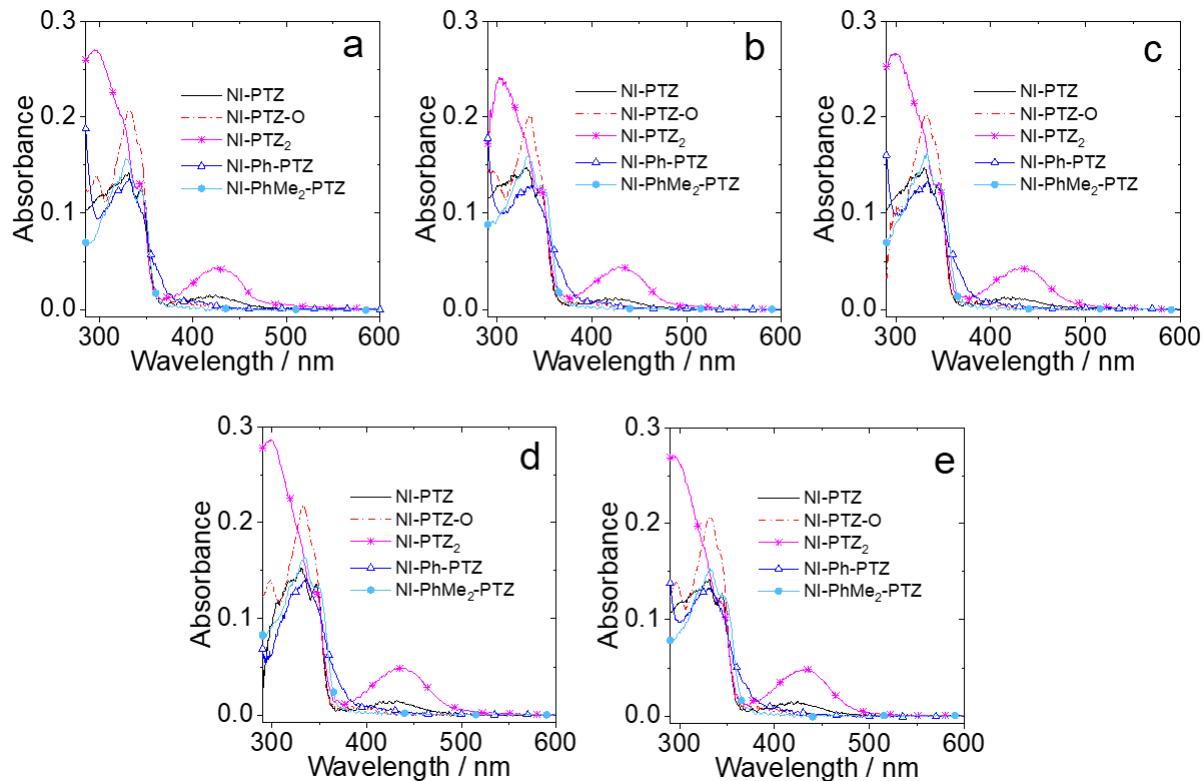


Figure S25. UV-vis absorption spectra of **NI-PTZ**, **NI-PTZ-O**, **NI-PTZ₂**, **NI-Ph-PTZ**, and **NI-PhMe₂-PTZ** in (a) cyclohexane (CHX); (b) toluene (TOL); (c) tetrahydrofuran (THF); (d) dichloromethane (DCM); (e) acetonitrile (ACN). $c = 1.0 \times 10^{-5}$ M, 20 °C.

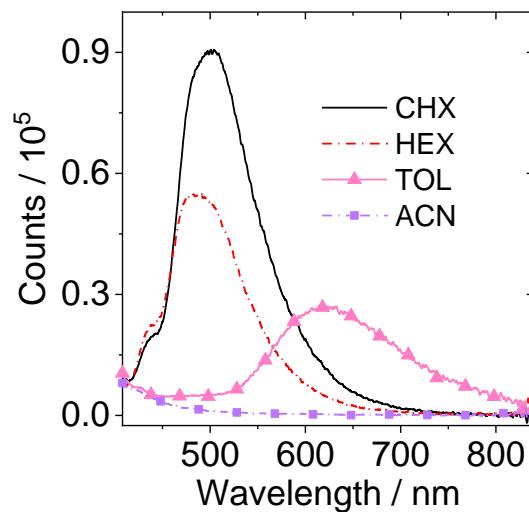


Figure S26. Fluorescence emission spectra of **NI-PhMe₂-PTZ** in different solvents. $A = 0.146$, $\lambda_{\text{ex}} = 330$ nm, 20 °C.

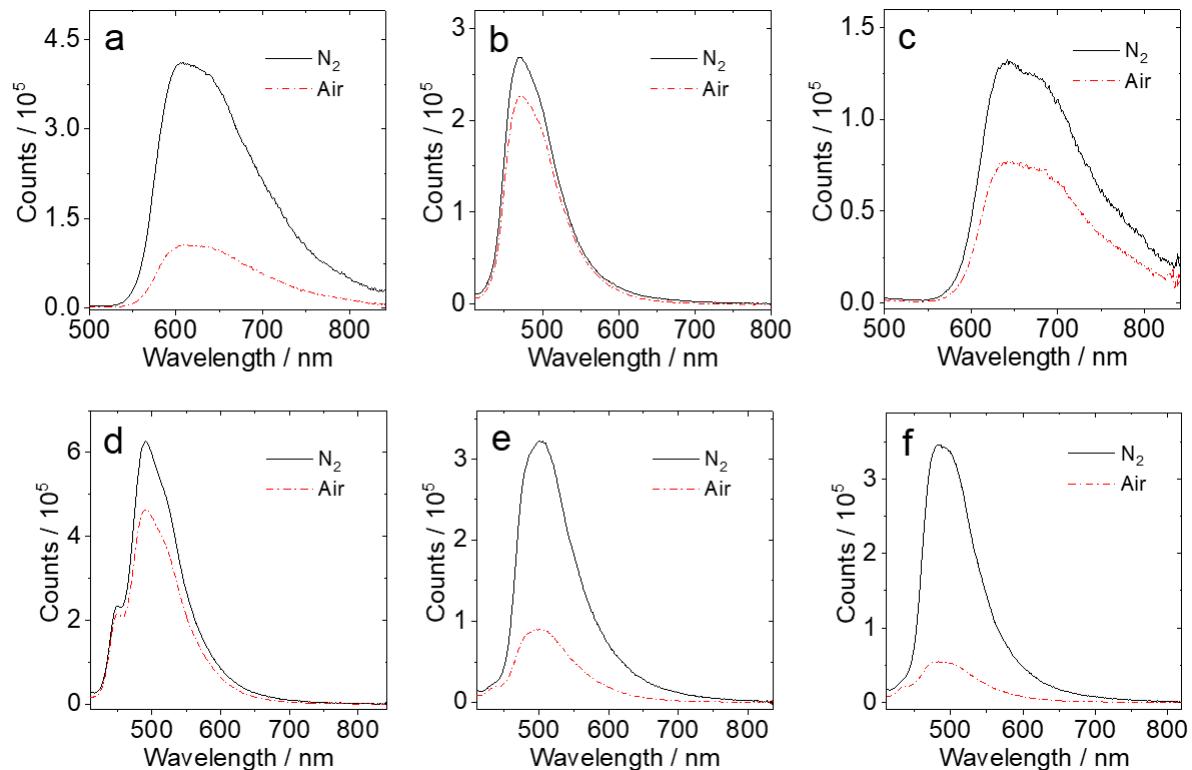


Figure S27. Fluorescence emission spectra of (a) **NI-PTZ**, (b) **NI-PTZ-O**, (c) **NI-PTZ₂**, (d) **NI-Ph-PTZ**, (e) **NI-PhMe₂-PTZ** in CYC, and (f) NI-PhMe₂-PTZ in *n*-HEX. Under different atmospheres (N₂, air). $A = 0.146$, $\lambda_{\text{ex}} = 330$ nm, 20 °C.

5. Fluorescence lifetimes

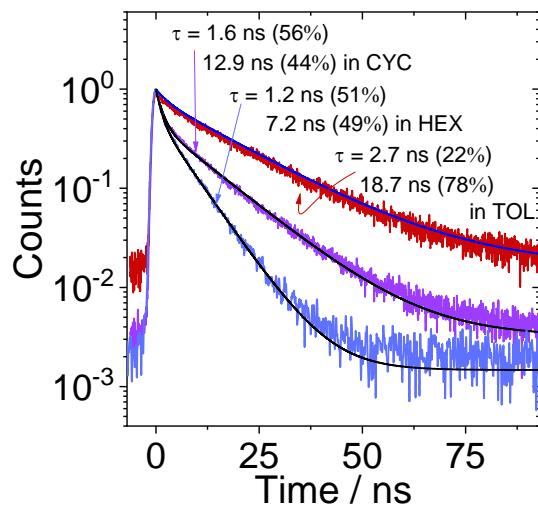


Figure S28. Decay traces of the luminescence of **NI-PhMe₂-PTZ** in different solvents.

Excited with picoseconds pulsed laser for fluorescence band ($\lambda_{\text{ex}} = 479 \text{ nm}$), $c = 1.0 \times 10^{-5} \text{ M}$, 20 °C.

6. Phosphorescence spectra

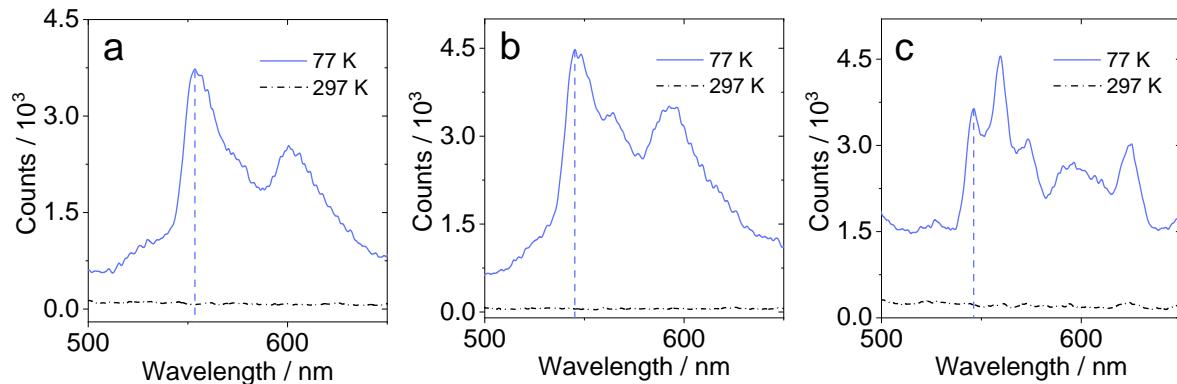


Figure S29. Phosphorescence spectra of the compounds (a) **NI-Ph-PTZ** ($\lambda_{\text{ex}} = 554 \text{ nm}$), (b) **NI-PhMe₂-PTZ** ($\lambda_{\text{ex}} = 545 \text{ nm}$), and (c) **NI-3Br** ($\lambda_{\text{ex}} = 547 \text{ nm}$) at 77 K, in 2-methyltetrahydrofuran, $c = 1.0 \times 10^{-5} \text{ M}$.

7. Phosphorescence lifetimes

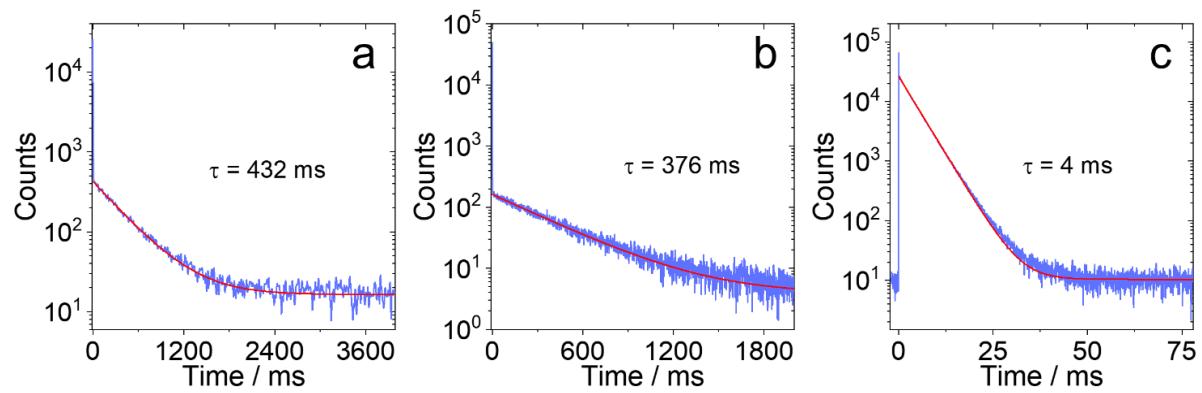


Figure S30. Decay traces of the phosphorescence of the compounds (a) **NI-Ph-PTZ** ($\lambda_{\text{ex}} = 554 \text{ nm}$), (b) **NI-PhMe₂-PTZ** ($\lambda_{\text{ex}} = 545 \text{ nm}$), and (c) **NI-3Br** ($\lambda_{\text{ex}} = 547 \text{ nm}$) in 2-methyltetrahydrofuran, $c = 1.0 \times 10^{-5} \text{ M}$, 77 K.

8. Spectroelectrochemistry measurement

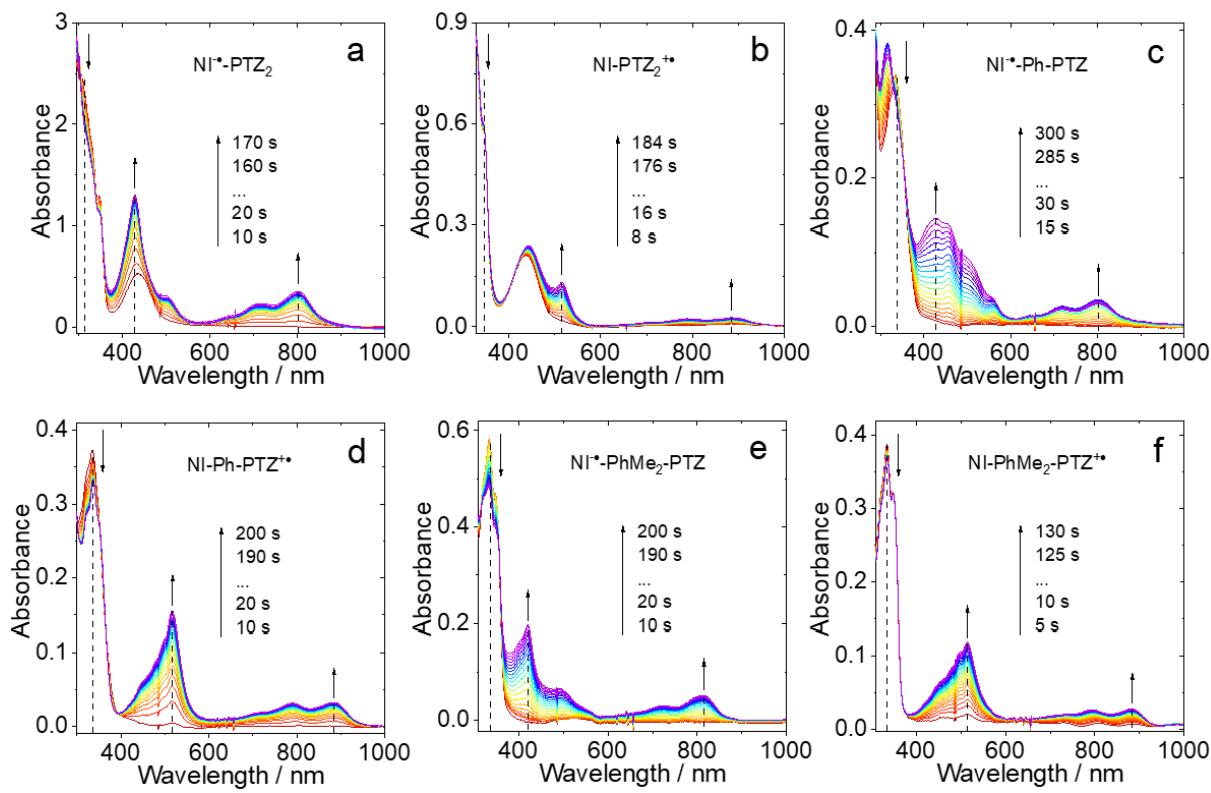


Figure S31. Spectroelectrochemistry traces of the UV–vis absorption spectra for (a) **NI-PTZ₂** observed from neutral (red) to monoanion (purple) at controlled potential of -1.83 V (vs. Ag/AgNO₃), (b) **NI-PTZ₂⁺** observed from neutral (red) to monocationic (purple) at controlled-potential of 0.53 V (vs. Ag/AgNO₃), (c) **NI-Ph-PTZ** observed from neutral (red) to monoanion (purple) at controlled potential of -1.85 V (vs. Ag/AgNO₃), (d) **NI-Ph-PTZ⁺** observed from neutral (red) to monocationic (purple) at controlled-potential of 0.55 V (vs. Ag/AgNO₃), (e) **NI-PhMe₂-PTZ** observed from neutral (red) to monoanion (purple) at controlled potential of -1.85 V (vs. Ag/AgNO₃), (f) **NI-PhMe₂-PTZ⁺** observed from neutral (red) to monocationic (purple) at controlled potential of 0.60 V (vs. Ag/AgNO₃). In deaerated dichloromethane containing 0.10 M Bu₄[NPF₆] as supporting electrolyte and with Ag/AgNO₃ as reference electrode, 20 °C.

9. Nanosecond transient absorption spectroscopy

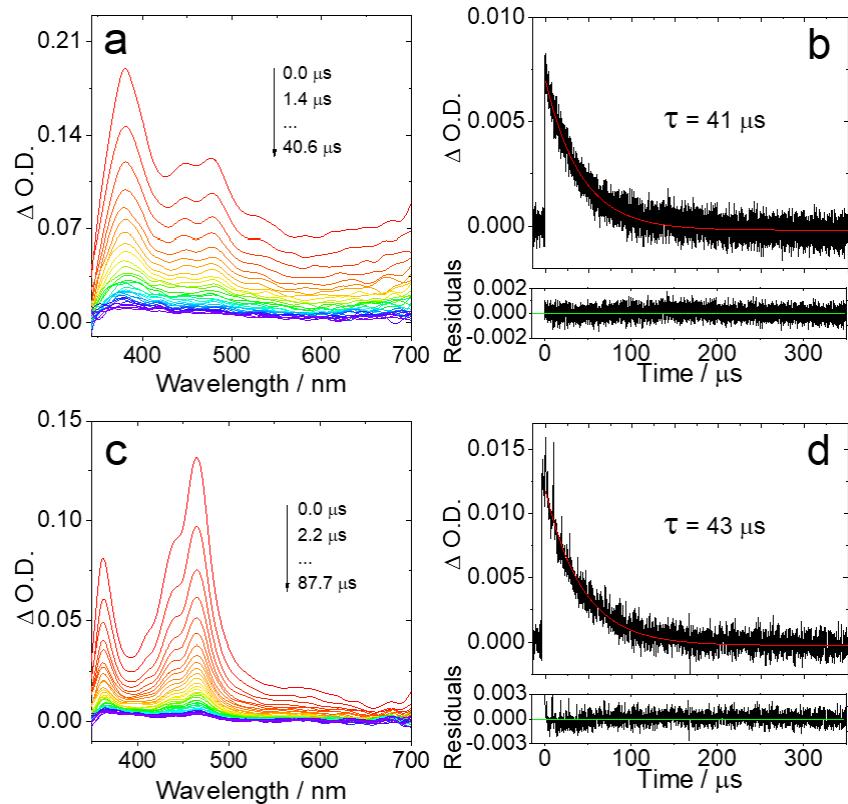


Figure S32. Nanosecond transient absorption of (a) **NI-Ph-PTZ** ($c = 5 \times 10^{-5}$ M) and (c) **NI-PhMe₂-PTZ** ($c = 5 \times 10^{-5}$ M). Decay traces of (b) **NI-Ph-PTZ** ($c = 2 \times 10^{-6}$ M) at 380 nm and (d) **NI-PhMe₂-PTZ** ($c = 2 \times 10^{-6}$ M). In deaerated HEX, $\lambda_{ex} = 355$ nm, 20 °C.

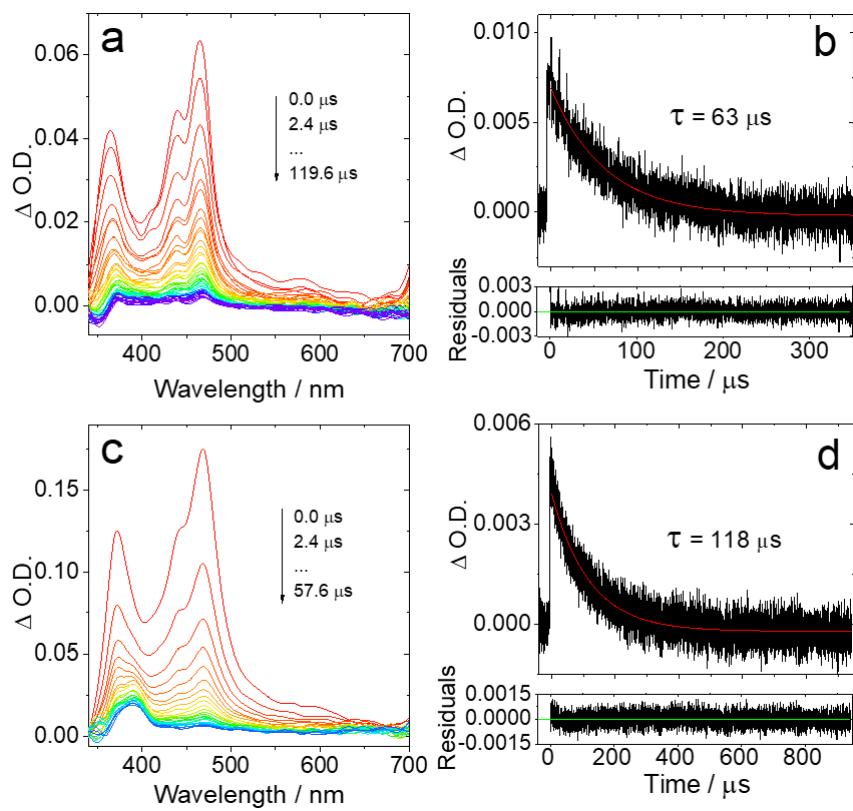


Figure S33. Nanosecond transient absorption of **NI-3Br** (a) $c = 3.0 \times 10^{-5}$ M in deaerated HEX and (c) $c = 1.0 \times 10^{-4}$ M in deaerated ACN. Decay traces of (b) $c = 2.0 \times 10^{-6}$ M in deaerated HEX and (d) $c = 1.0 \times 10^{-6}$ M in deaerated ACN at 470 nm. $\lambda_{ex} = 355$ nm, 20 °C.

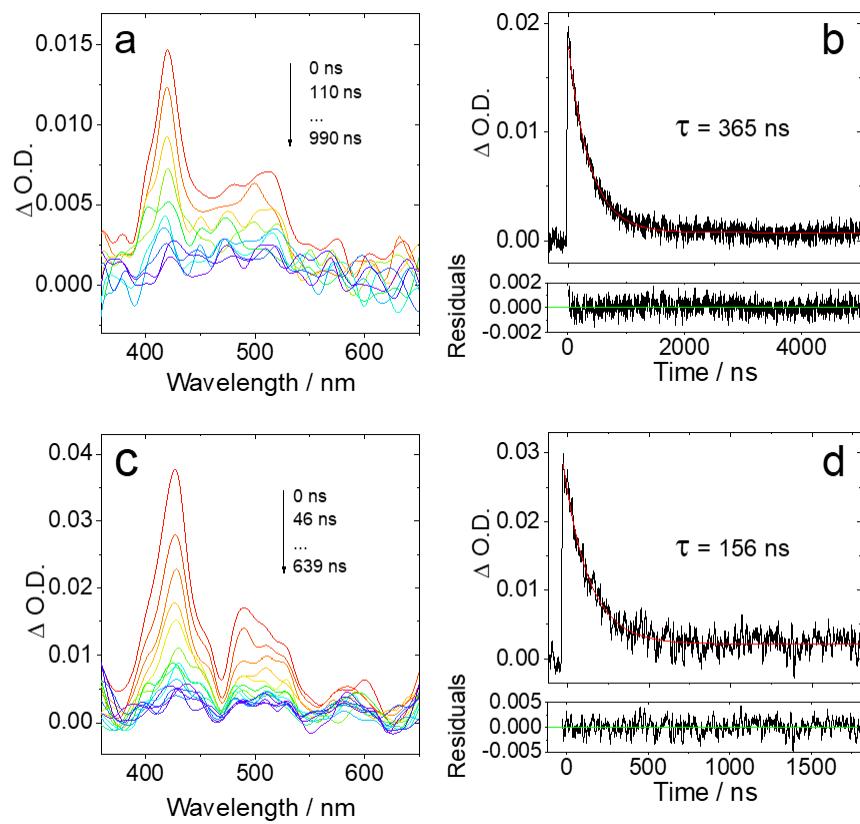


Figure S34. Nanosecond transient absorption of (a) **NI-PTZ** and (c) **NI-N-PTZ**. Decay trace of (b) **NI-PTZ** and (d) **NI-N-PTZ** at 420 nm. In deaerated ACN, $c = 1 \times 10^{-4}$ M, $\lambda_{\text{ex}} = 355$ nm, 20 °C.

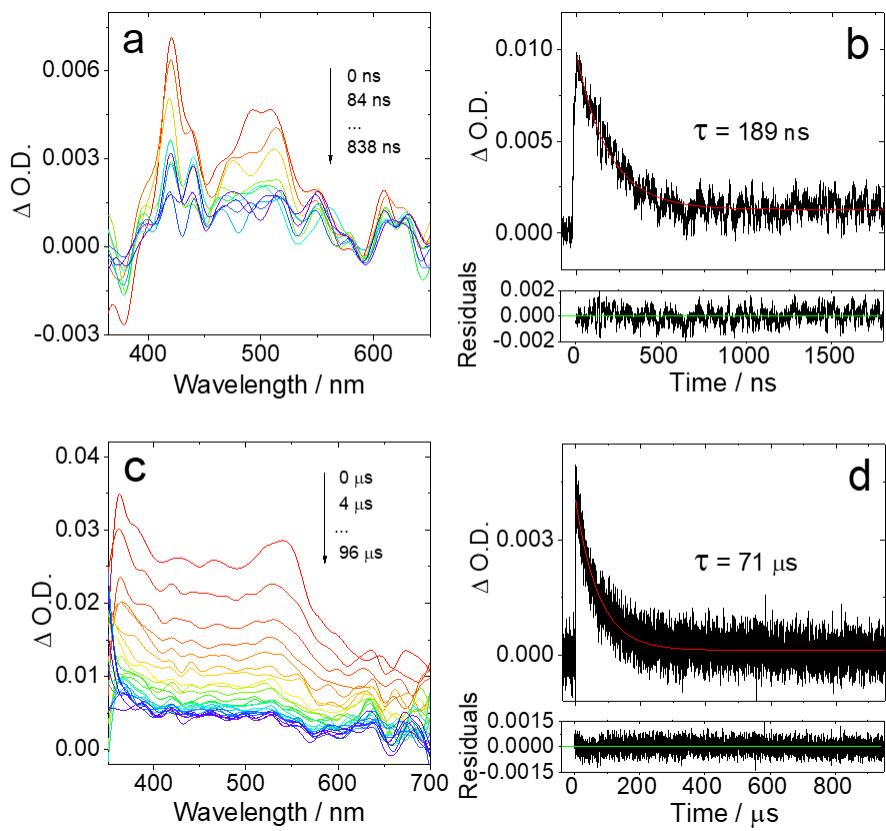


Figure S35. Nanosecond transient absorption of (a) **NI-PTZ₂** ($c = 1.0 \times 10^{-4}$ M) and (c) **NI-PTZ-O** ($c = 1.0 \times 10^{-5}$ M). Decay traces of (b) **NI-PTZ₂** ($c = 1.0 \times 10^{-4}$ M) at 420 nm and (d) **NI-PTZ-O** ($c = 1.0 \times 10^{-5}$ M) at 540 nm. In deaerated ACN, $\lambda_{\text{ex}} = 355$ nm, 20 °C.

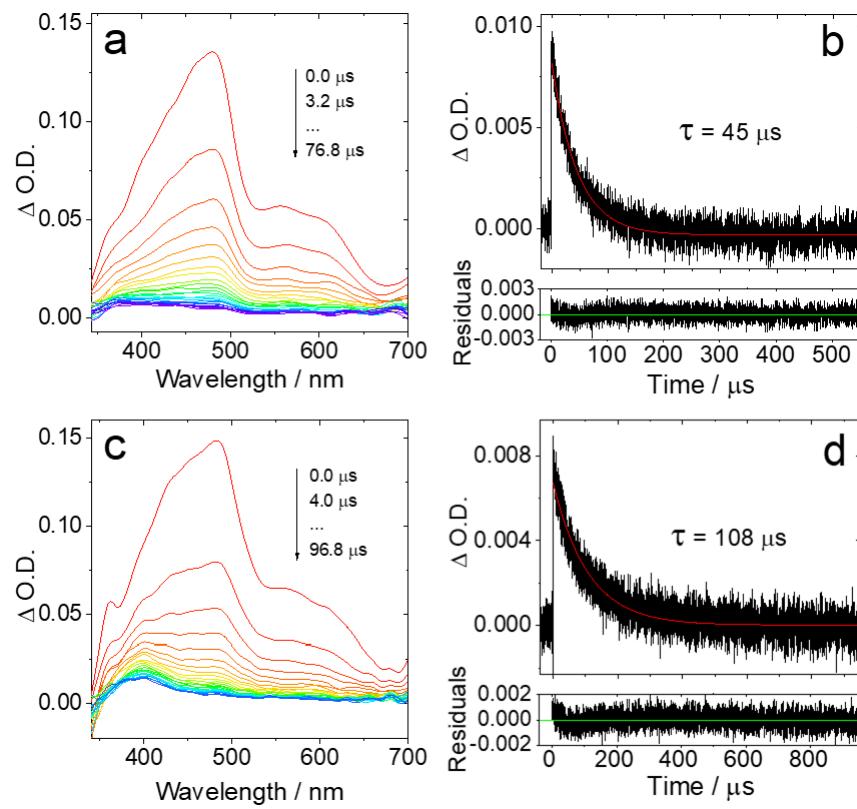


Figure S36. Nanosecond transient absorption of **NI-Ph-Br** (a) in HEX and (c) in ACN, $c = 5.0 \times 10^{-5}$ M. Decay traces of (b) in HEX and (d) in ACN, $c = 2.0 \times 10^{-6}$ M, $\lambda_{\text{em}} = 490$ nm. $\lambda_{\text{ex}} = 355$ nm, 20 °C.

10. Theoretical computation

Table S1. Vertical absorption of **NI-N-PTZ**, **NI-PTZ**, **NI-PTZ-O**, **NI-PTZ₂**, **NI-Ph-PTZ**, and **NI-PhMe₂-PTZ** (TDA-CAM-B3LYP/6-31G(d) in the gas phase, in eV) along with their oscillator strengths (f) and major orbital contributions. The energy levels and major orbital contributions for T₁ and T₂ at the Franck–Condon region are also given.

Compounds	S ₁ (absorption)				T ₁		T ₂	
	$E_{\text{abs}}(f)$ eV)	$f/10^{-4}$	C ^a MC ^{b,c}	ΔE_{vert} (eV) ^d	C ^a MC ^{b,c}	ΔE_{vert} (eV) ^d	C ^a MC ^{b,c}	
NI-N-PTZ	3.07	0	CT H–L (0.67)	2.69	LE H-2–L (0.65)	3.04	CT H–L (0.66)	
NI-PTZ	3.17	1	CT H–L (0.67)	2.73	LE H-2–L (0.67)	3.12	CT H–L (0.64)	
NI-PTZ-O	3.59	21	CT H–L (0.68)	2.74	LE H-2–L (0.67)	3.55	CT H–L (0.66)	
NI-PTZ₂	3.06	1	CT H–L (0.67)	2.72	LE H-4–L (0.64)	3.00	CT H–L (0.65)	
NI-Ph-PTZ	3.92	3	CT H–L (0.61)	2.67	LE H-2–L (0.61)	3.45	LE H–L+4 (0.36)	
NI-PhMe₂-PTZ	3.90	3	CT H–L (0.64)	2.71	LE H-2–L (0.66)	3.65	– H-4–L (0.56)	

^a Character; ^b Major contributions; ^c H and L represent HOMO and LUMO, respectively. Predominant HOMO→LUMO transitions for S₁, T₁, and T₂, between brackets the corresponding coefficient; ^d Δ_{vert} corresponds to the energy difference between GS and T₁ and T₂ at the FC region.

Table S2. Emission energies (TDA-CAM-B3LYP/6-31G(d) in the gas phase, in eV) along with their oscillator strengths (f) and major orbital contributions. The energy levels and major orbital contributions for S_1 , T_1 and T_2 are given at their respective optimal energy geometries.

Compounds	S_1 (emission)			T_1 (emission) ^e		T_2 (emission) ^e	
	E_{ems}	C^a	f^d	E_{ems}	C^a	E_{ems}	C^a
	/eV	MC ^{b,c}	/10 ⁻⁴	/eV	MC ^{b,c}	/eV	MC ^{b,c}
NI-N-PTZ	2.22	CT H-L	0	1.93	LE/CT H-1-L	-	-
		(0.69)			(c: 0.5)/H-L		
					(0.4)		
NI-PTZ	2.21	CT H-L	2	1.84	CT H-L	2.01	LE H(-2)-L
		(0.69)			(0.64)		(0.68)
NI-PTZ-O	2.86	CT H-L	1	2.02	LE H(-2)-L	2.83	CT H-L
		(0.68)			(0.68)		(0.67)
NI-PTZ₂	2.09	CT H-L	1	1.80	LE/CT H-1-L	-	-
		(0.69)			(0.63)		
NI-Ph-PTZ	3.00	CT H-L	0	2.01	LE H(-1)-L	-	-
		(0.65)			(0.66)		
NI-PhMe₂-	3.24	CT H-L	447	2.02	LE H(-1)-L	-	-
PTZ		(0.68)			(0.60)		

^aCharacter; ^bMajor contributions; ^cH and L represent HOMO and LUMO, respectively.

Predominant HOMO \rightarrow LUMO transitions for S_1 , T_1 , and T_2 , between brackets the corresponding coefficient; ^doscillator strengths, eV; ^e $f = 0$.

Table S3. Calculated energy gaps at different regions of the photo deactivation decay (in eV) for **NI-PTZ** and **NI-PTZ-O**.

Molecule	$\Delta E_{S, T-GS}$ (eV) ^a			ΔE_{S-T} (eV)		ΔE_{T-GS} (S_1 , eV) ^b		ΔE_{S-T} (S_1 , eV)	
	1CT	3LE	3CT	$^1CT-$	$^1CT-$	3LE	3CT	$^1CT-$	$^1CT-$
				3LE	3CT			3LE	3CT
NI-PTZ	2.60	2.37	2.14	0.23	0.46	2.74	2.57	-0.14	0.03
NI-PTZ-O	3.12	2.37	3.09	0.75	0.03	2.63	3.09	0.49	0.03

O

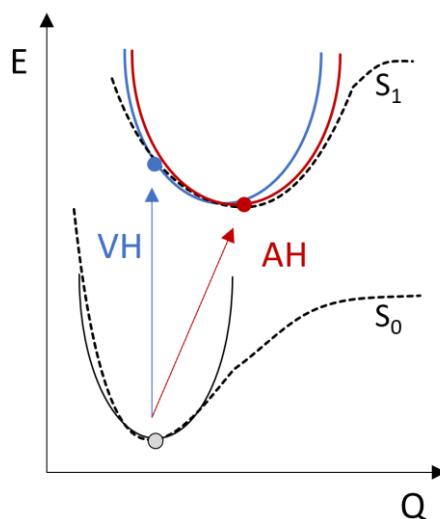
^a $\Delta E_{S, T-GS}$ corresponds to the energy difference between the singlet (S) or triplet (T) minimum and the ground state (GS) minimum, i.e., adiabatic energy difference;

^bRelative energies at the S_1 optimized geometry, i.e., vertical energy difference.

Vibronic models

For the rate calculations, the Franck–Condon factors, $\langle v_i | v_f \rangle$, are computed by constructing the vibrational wavefunction as a sum of harmonic oscillators for both the initial and final state. Both these states are considered in the same reference frame, making it possible to connect them through translation and rotation of one of the states. This is accomplished by using the Duschinsky rotation effect (DRE), mapping the normal modes of one state onto the modes of the other state [4,5]. Here, a distinction can be made depending on how to approximate the harmonic normal modes from each state [6]. In vertical models, the same geometry is used for both initial and final state modes, while in adiabatic models the respective minima of both states are used for such a purpose. In addition, one could choose to calculate the gradient and/or hessian at only one or at both states. Representing a final state hessian by an initial state hessian will result in major errors, such that the adiabatic and vertical hessian (AH and VH, see exemplarily for ground and first excited state in Scheme S1) models, which

both use the Hessians from both the initial and the final states, are the only ones suitable for accurate calculations [6,7].



Scheme S1. Visualization of the adiabatic (AH) and vertical hessian (VH) models.

Activation energies from the computed adiabatic energy difference gaps and reorganization energies

According to [8], the activation energy for the RISC process (ΔG) can be obtained with

$$\Delta G = \frac{(\Delta E_{if} - \lambda)^2}{4\lambda}$$

where for a RISC ΔE_{if} corresponds to $-\Delta E_{S-T}$ (see values in Table S3) and λ corresponds to the reorganization energies between the initial and final states.

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